

**Towards accurate calculations of  $\text{Zn}^{2+}$  binding free energies  
in zinc finger proteins**

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## Abstract

Zinc fingers are  $\text{Zn}^{2+}$ -bound peptide motifs that bind DNA specifically and have great potential in gene therapy. However, the ion binding strength of the zinc finger is not well known, and computing this quantity will allow for the design of more stable zinc finger treatments. Ions in solution are a model system. Molecular dynamics (MD) simulations and the inverse potential distribution theorem were used to estimate the solvation free energies of zinc ions. The zinc coordination shells were stable and the initial coordination shell stayed throughout the 20 *ns* simulations. Quasi-chemical (QC) calculations are free energy calculations that partition the system into an inner shell, treated using quantum mechanics, and an outer shell, treated using continuum electrostatics. The theory was extended to multiple ligands in solution and used on  $\text{Zn}^{2+}$  in water/methanol mixtures, with the inner shell consisting of the six solvent molecules coordinated to the ion and the outer shell consisting of all other solvent. Increasing methanol coordinated to the zinc led to lower inner shell formation free energies but higher outer shell free solvation energies. A six-water coordination shell was found to be most stable. Using quasi-chemical theory with different concentrations in the outer shell did not yield major differences, but this could have been due to an insufficient treatment of the van der Waals forces. A quasi-chemical approximation using MD to treat the outer shell would fix such problems and will be useful in computing zinc finger ion binding free energies.

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# 1 Introduction

Metal ions are important biologically because of their structural and reactive role in many proteins. It is estimated that one-third of all proteins are metalloproteins (metal-containing proteins) [1]. They play important roles in reduction/oxidation reactions due to their electron transfer properties. Their highly charged nature also enhances the structural stability of many proteins. One class of such metalloproteins are zinc finger proteins.

Zinc finger proteins are DNA binding proteins with structural  $\text{Zn}^{2+}$  ions that have demonstrated a high degree of specificity for certain DNA strands. Because of this, they have found applications in gene therapy, as they can be attached to nucleases and used to excise specific DNA sequences. Some researchers have recently demonstrated success in using zinc-finger nucleases to treat viral diseases such as HIV [2] and Hepatitis B [3] by destroying their DNA or required cellular co-receptors. However, the role of the divalent ion in the stability of the protein is not well known. Understanding the effect of mutations on the thermodynamic stability of the  $\text{Zn}^{2+}$  ion in the zinc finger allows for more stable synthetic zinc fingers to be constructed, increasing the ease and efficacy of using zinc-finger nucleases and other similar therapeutics. Also, as highly specific zinc-binding proteins, these could be used with an embedded fluorescent group as a sensitive zinc detector [4]. Understanding the comparative thermodynamic stability of such a protein to other ions will allow for the development of better models of metalloprotein binding.

Modern experimental methods, such as X-ray diffraction (XRD) and nuclear magnetic resonance (NMR) allow for the characterization of crystal structures. However, XRD cannot be used to determine solution structures, as the protein must be crystallized. Computer simulations must be used to solvate such structures. NMR can be used to determine solution structures, but computer simulations are used to refine such structures to yield more accurate descriptions of the protein conformation. One of the major computer simulation methods used is molecular dynamics (MD). MD simulations are atomistic simulations that use classical mechanics to determine trajectories of the atoms from an initial configuration. These simulations allow for the refinement of experimental structures as well as determination of basic thermodynamic quantities such as solvation free energies and interaction energies. The atomistic nature of MD simulations also allows insight into the mechanisms of atomic processes. MD simulations can be used to generate trajectories that are several *ns* in length for systems with tens of thousands of atoms. However, for metal ions, classical molecular dynamics simulations are unable to capture the quantum mechanical effects such as charge transfer and polarization. Other computational models must be used to accurately simulate the behavior of the metal ion.

Another method of computational structure determination is based on electronic structure theory. Quantum mechanical (QM) calculations, also known as *ab initio* calculations, derive results from the wavefunctions of the electrons in the system by solving self-consistent field equations. Thermodynamic properties can then be calculated from those wavefunctions using the harmonic approximation [5]. In general, this method is more accurate for calculating structural and thermodynamic properties than molecular dynamics, but is much more computationally demanding. Because of this limitation, QM calculations are only feasible for small systems on the order of tens of atoms. Also, QM does not capture the dynamics of the system. Newer methods such as *ab initio* molecular dynamics (AIMD) are able to perform dynamics

on such systems, but can only be feasibly used with tens of atoms over periods of under 1 *ns*.

In order to simulate systems with hundreds of atoms accounting for quantum effects on nanosecond timescales, several methods have been devised to link quantum calculations with faster approximations. One is the hybrid quantum mechanics/-molecular mechanics (QM/MM) method [6], where a subset of the atoms are treated with quantum mechanics and the rest of the atoms are treated using molecular (classical) mechanics. The two types of simulations are linked together using link atoms that are treated both ways and are attached to atoms from both sets. However, this method is not yet feasible for generating trajectories of protein simulations (tens of thousands of atoms) of sufficient length (several *ns*) for determining thermodynamic properties.

Another method is the quasi-chemical approximation [7], which partitions molecules into an inner shell and an outer shell. Under this model, the process of solvation can be decomposed into two parts: the formation of the inner shell and the solvation of the inner shell in the outer shell. Quantum mechanics are used to calculate free energies of formation of the inner shell complex, and the free energy of solvation is determined using continuum electrostatics. This method has been used with success on ions in water [8]. Such an approximation is much faster than any quantum simulation, yet also allows for accurate determination of free energies of solvation. However, this approach has not been used for mixtures of water and other solvents, which is a plausible model for considering a protein as a "solvation shell" for an ion.

## 2 Methods

### 2.1 Theory

#### 2.1.1 Molecular Dynamics Simulations

Molecular dynamics simulations represent each atom as a point charge and mass with a Lennard-Jones 12-6 potential for van der Waals type forces. Interaction energies are provided from force fields and numerical integration is used to predict movement of atoms, generating an ensemble of states. Free energies can be calculated from these simulations using the principles of statistical mechanics. From the inverse potential distribution theorem [7], the excess chemical potential of a molecule  $X$  is

$$\mu_X^{ex} = \frac{1}{\beta} \log \left[ \int_{-\infty}^{\infty} e^{\beta\epsilon} P_X(\epsilon) d\epsilon \right] \quad (2.1)$$

where  $\beta = \frac{1}{k_B T}$ ,  $\epsilon$  is the interaction energies between  $X$  and all other species, and  $P_X$  is the probability density function of  $\epsilon$ . Assuming a gaussian distribution for the energies ( $P_X(\epsilon) \propto e^{-\frac{(\epsilon - \langle \epsilon \rangle)^2}{2\sigma^2}}$ ) and substituting this into Equation 2.1 results in

$$\mu_X^{ex} = \langle \epsilon \rangle + \frac{\beta\sigma^2}{2} \quad (2.2)$$

#### 2.1.2 Quantum Mechanical Calculations

In QM calculations, an initial geometry is specified, and the wavefunctions of the electrons are solved to determine the internal energy of the system. The second derivatives of the energy functions can then be analyzed to determine the electronic vibrational structure of the system. Such frequency calculations can then be used to determine free energies of formation based on the harmonic approximation [5].

The method of solving the wavefunctions used in this case is density functional theory (DFT), where functionals of the spatial density of electrons are derived from

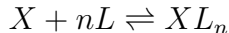
experiment or higher-level ab initio calculations. Since the functionals contain information about different atoms, such an approach is faster than pure ab initio approaches, which do not consider such information.

### 2.1.3 Continuum electrostatics

In lieu of explicit solvent, solvent effects can be accounted for by treating them from an electrostatics perspective. This is due to the fact that at the distances considered as the outer shell (several Å), the van der Waals forces are typically much smaller than the electrostatic interaction with the zinc ion. The generalized Born solvation model [9] was used for the determination of the free energy changes. In this model, the free energy of solvation is approximated as the free energy of taking a charged object of a certain shape from a medium with a dielectric constant of 1 to a medium with the dielectric constant of the desired solvent.

### 2.1.4 Quasi-Chemical Model

In the quasi-chemical approximation, we decompose the system into two parts: we define an inner shell and an outer shell, and combine the two to determine the solvation free energy. The contribution of the outer shell is defined as the solvation free energy of the complex, and can be calculated using continuum electrostatics. The free energy of the inner shell is defined chemically: given a species  $X$  and ligand  $L$ , the free energy of the formation of a cluster  $XL_n$  is the free energy change of the following reaction:



This is equivalent to the expression  $-kT \ln K_n^{(0)}$ , where  $K_n^{(0)}$  is the ideal gas reaction rate constant at 1 atm and 298 K. This value can be calculated using QM methods. In the case of ions in solvent, the  $X$  is the ion species, and the  $L$  are the solvent molecules around the ion. A more thorough derivation of quasi-chemical theory can

be found in [7].

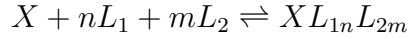
The free energies are calculated in an ideal gas state at 298  $K$  and 1  $atm$ , but we are interested in the liquid state. To correct for this state, the free energy change due to a pressure change is  $nkT \ln \left( \frac{P_{liq}}{P_0} \right)$ , where  $P_{liq}$  is  $RT\rho_w$  and  $\rho_w$  is the molar density of the solvent. This yields the ideal gas pressure at liquid densities.  $P_0$  is 1  $atm$ . This term is also written as  $-kT \ln \rho^n$ , as it is a density factor, and can be combined with the previous term as  $-kT \ln K_n^{(0)} \rho^n$ . A further discussion on this topic can be found in Grabowski et al [10].

A particular species  $X$  may also have coordination shells with different  $n$ . In that case, a term  $kT \ln p_X(n)$  is included, where  $p_X(n)$  is the probability of  $X$  being coordinated by  $n$   $L$ 's. This term accounts for the fact that this particular arrangement only contributes partially to the free energy. A first-order approximation is to consider only the most probable coordination number  $\tilde{n}$ . A more thorough discussion of this term can be found in Asthagiri et al [11].

Combining these terms together results in the expression

$$\mu_X^{ex} = -kT \ln K_{\tilde{n}}^{(0)} \rho^{\tilde{n}} + kT \ln p_X(\tilde{n}) + (\mu_{XL_{\tilde{n}}}^{ex} - \tilde{n} \mu_L^{ex}) \quad (2.3)$$

To extend this method to multiple ligand species, we can consider two ligands,  $L_1$  and  $L_2$ . The reaction is then



For a first order approximation of the density factor, one can calculate the density of the solution by assuming that this is an ideal solution and approximating the liquid molar density as  $\rho_{L_1L_2} = x_{L_1}\rho_{L_1} + x_{L_2}\rho_{L_2}$ . This leads to  $P_{L_1L_2} = kT\rho_{L_1L_2}$ . Although this may not be true, the effect of the term is not very significant in the calculations (see Section 3.2.4). A more accurate approximation could also be per-

formed considering excess molar volumes. The corresponding density factor is then  $(n + m) kT \ln \left( \frac{P_{L_1 L_2}}{P_0} \right)$ . Like before, we may write  $\frac{P_{L_1 L_2}}{P_0} = \rho$ . The probability term can be modified to account for changes in the coordination numbers of  $n$  and  $m$ . The free energy is then determined to be

$$\begin{aligned} \mu_X^{ex} = & -kT \ln K_{n,m}^0 \rho^{(n+m)} + kT \ln p_X(n, m) \\ & + (\mu_{X L_1 n L_2 m}^{ex} - n \mu_{L_1}^{ex} - m \mu_{L_2}^{ex}) \end{aligned} \quad (2.4)$$

## 2.2 Calculation details

All calculations were performed on the GLENN cluster of the Ohio Supercomputer Center on dual socket nodes with two quad-core 2.5 GHz AMD Opteron processors. Calculation files can be found in Appendix A. More details on the specific calculations performed can be found in the Results section (Section 3).

### 2.2.1 Ions in solution

Simulation files were prepared using VMD 1.8.7 and the solvate plugin. A PDB file containing one ion was created by hand and solvated with a 32 Å TIP3P water box.

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and the CHARMM 27 force field. The force field file can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were used. The nonbonded cutoff was set at 12 Å. Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters and methanols were constrained with the SHAKE algorithm. The system was minimized at 0K for 7500 steps, velocities were reinitialized to 298K, and the system was equilibrated for 200 ps. Production runs of 20 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames

in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

A QM calculation of the  $\text{Zn}^{2+}$  ion was performed. DFT calculations were performed using Gaussian 09 Revision A.01 [13]. The Becke three-parameter Lee-Yang-Parr (B3LYP) hybrid exchange-correlation functional and the 6-311++G(2d,p) basis set was used. Initial structures were obtained from MD simulations. Structures were first optimized on a 6-31+ basis set, then on a 6-311+G(d,p) basis set, and finally on the 6-311++G(2d,p) at the VeryTight optimization level. Free energies were obtained using frequency analysis on optimized structures. No imaginary frequencies were found, indicating stable structures. Population analysis according to the CHELPG [14] procedure was used to determine charges. Radii for the different atoms were taken from Stefanovich et al [15]. The radius for  $\text{Zn}^{2+}$  was set at 2.2 Å, as the value did not change the calculation much. Free energies of solvation were then calculated according to the generalized Born solvation model using the Adaptive Poisson-Boltzman Solver (APBS) 1.3 [16].

### 2.2.2 $\text{Zn}^{2+}$ in methanol/water solutions

Coordination shells with specific numbers of methanols and waters were created by hand-modifying a PDB file generated from the QM optimization of the  $\text{Zn}^{2+}$  ion above. These were energy-minimized at 0 K in NAMD using the OPLS-ua force field to produce optimized structures. The force field file can be found in A.2. The optimized structures were put in a 2500-atom methanol/water solvent box with 0%, 5%, 10%, 15% or 100% MeOH mol% using PACKMOL [17].

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and the OPLS-ua force field. The force field file can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were



used. The nonbonded cutoff was set at 12 Å. Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters and methanols were constrained with the SHAKE algorithm. The system was minimized at 0K for 7500 steps, velocities were reinitialized to 298K, and the system was equilibrated for 200 ps. Production runs of 20 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

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### 2.2.3 $\text{Zn}^{2+}$ in zinc finger protein

The zinc finger motif used consisted of residues 42 to 71 of chain A of the TFIID zinc finger (PDB: 1TF6). The zinc finger motif was extracted from the NMR structure, and then hydrogen atoms were added using the PSFGEN module of VMD 1.9.1 [18]. The histidine residues coordinated to the zinc were changed to the neutral (HID) form and the cysteine residues were deprotonated. The protein was then solvated in

a  $48\text{\AA} \times 48\text{\AA} \times 54\text{\AA}$  TIP3P water box.

Molecular dynamics simulations were performed using NAMD 2.6b software [12] and two force fields. The CHARMM 27 force field modified to include a deprotonated cysteine, which was obtained from parameters for methylthiolate. The AMBER FF09 force field was not modified. The force field files can be found in Appendix A.2. NAMD input files can be found in Appendix A.3. Long-range electrostatics were treated using particle mesh Ewald (PME) and periodic boundary conditions were used. The nonbonded cutoff was set at  $12\text{\AA}$ . Langevin bath and a Nose-Hoover barostat at 298 K and 1 atm were used to generate NPT ensembles. A 2 fs timestep was used. Waters were constrained with the SHAKE algorithm. The system was minimized at 0K for 10000 steps and then heated from 0 K to 298 K over 50 ps and equilibrated for 200 ps. Production runs of 10 ns were performed. Frames were sampled every 250 fs. Pair interaction energies of the different frames in the trajectory were calculated using NAMD. The free energy was then calculated according to Equation 2.2 using MATLAB R2011b.

DFT calculations were performed using Gaussian 09 Revision A.01 [13]. The Becke three-parameter Lee-Yang-Parr (B3LYP) hybrid exchange-correlation functional and the 6-311++G(2d,p) basis set was used. Initial structures were obtained from the NMR structure. Structures were first optimized on a 6-31+ basis set, then on a 6-311+G(d,p) basis set, and finally on the 6-311++G(2d,p) at the VeryTight optimization level. Free energies were obtained using frequency analysis on optimized structures. No imaginary frequencies were found, indicating stable structures. Population analysis according to the CHELPG [14] procedure was used to determine charges. Radii for the different atoms were taken from Stefanovich et al [15]. The radius for  $\text{Zn}^{2+}$  was set at  $2.2\text{\AA}$ , as the value did not change the calculation much. Free energies of solvation were then calculated according to the generalized Born solvation model using the Adaptive Poisson-Boltzman Solver (APBS) 1.3 [16].

QM/MM calculations were performed using NWCHEM 6.1 [19]. The  $\alpha$ -carbons of the coordinating protein residues were considered to be the boundary of the QM region. The rest of the protein and a water shell were considered using molecular mechanics. The Amber FF09 force field was used for the MM portion. DFT using the LANL08DZ basis set, which is optimized for transition metals, was used with the B3LYP hybrid functional. Hydrogen link atoms were used. Optimization was performed using the conjugate gradient algorithm. The QM/MM boundary cutoff was set at 9 Å. Electrostatic potential fitting of the QM region was used for parameterization of the QM atoms during the MM optimization. Ten cycles of optimization were performed, with a maximum of 50000 solvent iterations, 10000 protein iterations, and 500 QM core iterations. The resulting optimized structure was then further refined using the DFT calculation methodology above except with the alpha carbons fixed at the optimized positions.

### 3 Results

#### 3.1 Ions in solution

##### 3.1.1 MD simulations of $\text{Na}^+$ , $\text{K}^+$ and $\text{Zn}^{2+}$ in water

MD simulations of ions in water were performed to verify that results obtained from NAMD were accurate. Interaction energies of the ion with the waters were calculated and fitted to a normal distribution (see Figure 1 and Figure 2).

From these plots, it was determined that the energies were indeed normally distributed, so the free energies were calculated using Eqn 2.2. Results for the different ions ( $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{Zn}^{2+}$ ) are tabulated in Table 1.

The experimental and quasi-chemical values were from Asthagiri et al [8]. From these calculations, it becomes evident that although the free energies calculated using

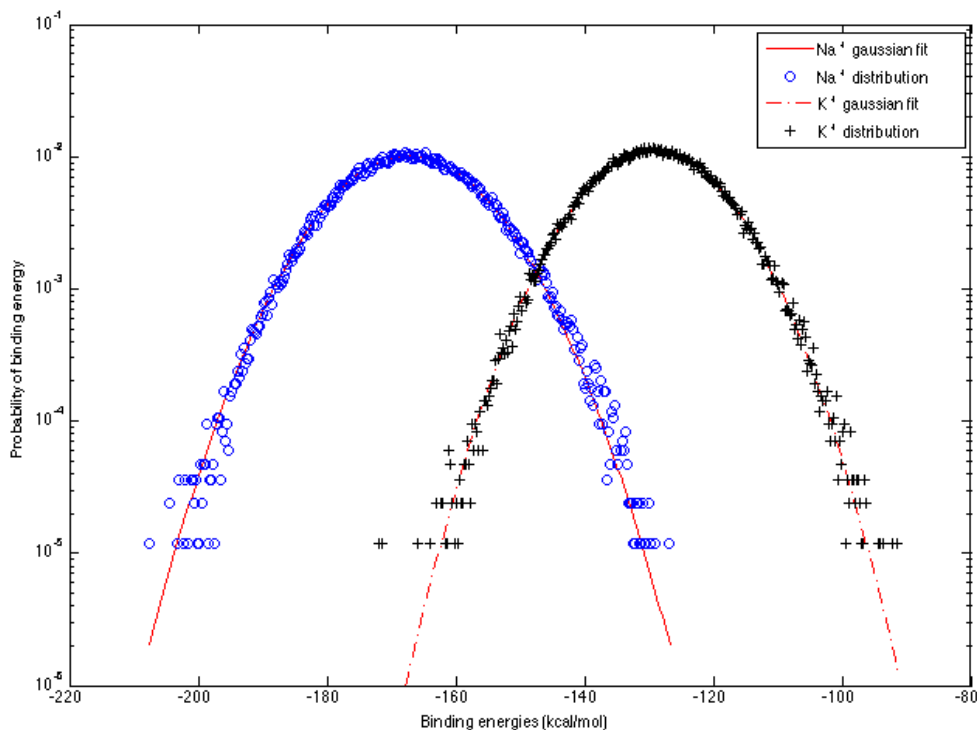


Figure 1:  $\text{Na}^+$  and  $\text{K}^+$  interaction energy distributions and gaussian fits from MD simulations.

this method are reasonable, the error increases with increasing atomic number and may be larger than desired. Because of this, a more accurate method will be used to determine free energies.

### 3.1.2 Quasi-chemical calculation of $\text{Zn}^{2+}$ hydration free energy

Quasi chemical theory was applied to the zinc ion in particular to determine more accurate binding free energies. The inner shell radius was determined from the first minimum of the  $\text{Zn}^{2+}$ -O radial distribution function (see Figure 3). The radial distribution function was calculated from the MD simulations of  $\text{Zn}^{2+}$  in water.

It was found to contain 6 water molecules. Trajectory analysis determined that the waters coordinating the ligands did not exchange, thus there was a sharply-defined inner shell. QM calculations of the core were then performed according to

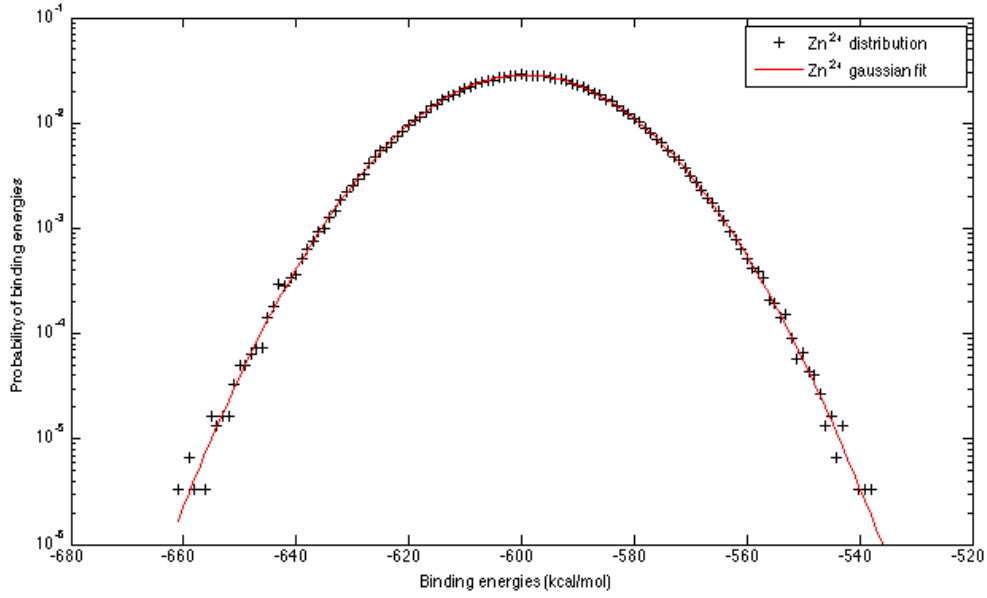


Figure 2:  $\text{Zn}^{2+}$  interaction energy distribution and gaussian fit from MD simulation.

Table 1: Solvation free energies for ions in water using MD compared to experimental values and quasi-chemical values

Units in $\left(\frac{\text{kcal}}{\text{mol}}\right)$	$\langle\epsilon\rangle$	$\beta\frac{\sigma^2}{2}$	$\mu_X^{ex}$	QC [8]	Exp. [8]
$\text{Na}^+$	$-166.9 \pm 0.3$	$81.8 \pm 1.4$	$-85.1 \pm 1.5$	-96.1	-91.5
$\text{K}^+$	$-129.3 \pm 0.2$	$67.2 \pm 0.6$	$-61.9 \pm 0.5$	-75.2	-74.6
$\text{Zn}^{2+}$	$-598.9 \pm 0.2$	$165.2 \pm 1.5$	$-433.8 \pm 1.5$	-458.1	-471.1

Standard deviations of values from dividing the simulation into 4 time blocks follow  $\pm$ .

the methodology in 2.2.3. The zinc solvation free energy and different components of the quasi-chemical free energy of solvation expression (Equation 2.3) can be found in Table 2.

The results agreed rather well with the results from Asthagiri et al [8].

### 3.2 $\text{Zn}^{2+}$ in methanol / water mixtures

In order to extend quasi-chemical theory to mixtures, the  $\text{Zn}^{2+}$  ion was solvated in mixtures of methanol and water. Parameters for these simulations were derived from

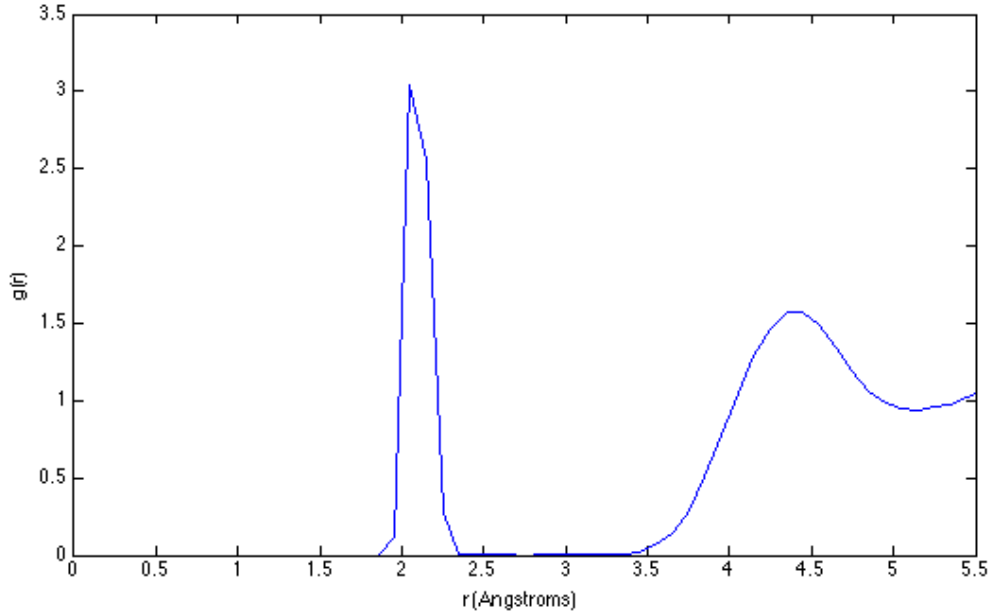


Figure 3:  $\text{Zn}^{2+}$ - $\text{OH}_2$  radial distribution function

Table 2: Quasi-chemical calculation of  $\text{Zn}^{2+}$  hydration free energy

$\left(\frac{\text{kcal}}{\text{mol}}\right)$	$-kT \ln K_n^{(0)}$	$\mu_{XL_n}^{ex}$	$\mu_L^{ex}$	$\mu_X^{ex}$	Experimental [8]
Asthagiri et al [8]	-279.2	-199.3	-7.7	-458.1	-471.1
This work	-282.8	-202.6	-8.1	-462.4	-471.1

the Optimized Potentials for Liquid Simulations United-Atom (OPLS ua) force field. In this force field, the methyl group of the methanol was approximated as a united atom. Simulations of 2500 solvent atoms and a zinc ion were run at methanol mol% of 0%, 5%, 10%, 15%, and 100%. It was found that the  $\text{Zn}^{2+}$  ion bound the six atoms around it from the initial configuration very tightly: no atoms coordinated to the zinc ion after minimization exchanged with other atoms in any of the 20 ns NPT production runs at any methanol mole fraction. Based on these results, MD simulations of the  $\text{Zn}^{2+}$  ion in water were performed with different coordination shells containing  $i$  waters and  $6 - i$  methanols for  $i$  ranging from 0 to 4.

### 3.2.1 Free energies of solvation

Interaction energies between the zinc ion and the all outer shell (non-coordinated solvent) were calculated. The energies were normally distributed. A sample energy histogram can be found in Figure 4.

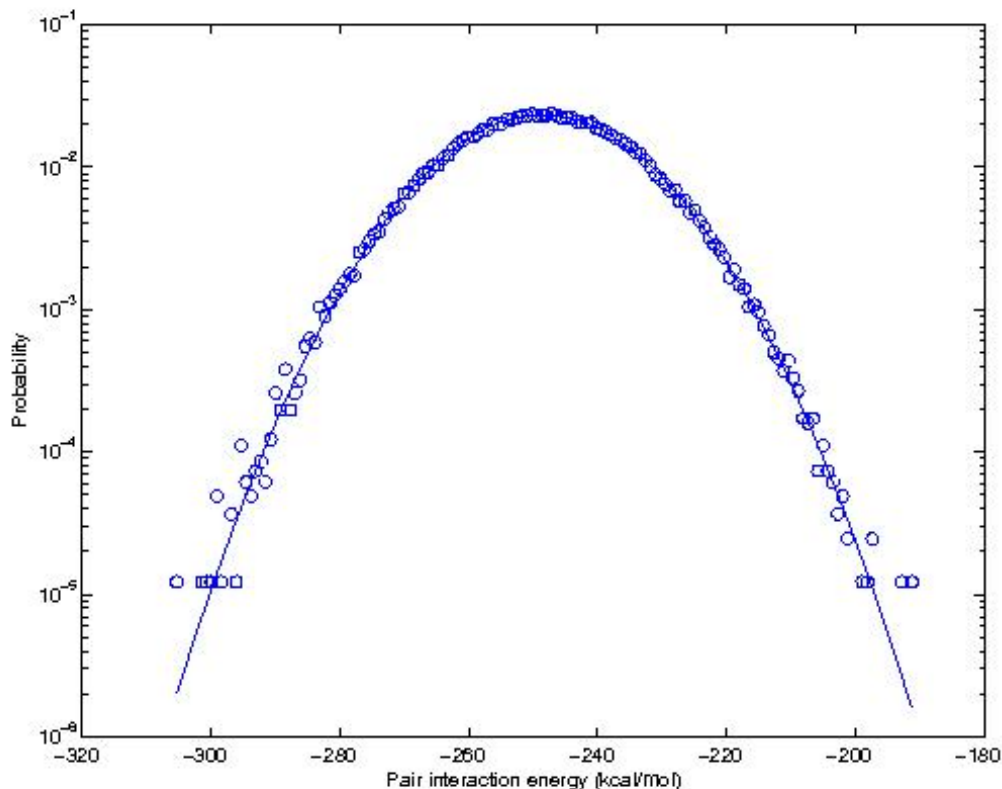


Figure 4: Interaction energy distribution of  $\text{Zn}^{2+}$  with non-coordinated solvent molecules (outer shell radius:  $3.5 \text{ \AA}$ ) in 15% MeOH and water

Histograms for the other systems can be found in Appendix C.2. The gaussian approximations of the interaction energy distributions were deemed valid, and the solvation free energies were calculated with Equation 2.2. The free energies of solvation are tabulated in Table 3.

Table 3: Calculation of  $\text{Zn}^{2+}$  ion solvation free energies from MD simulations for various solvents

Inner shell methanols	Methanol mol%	Zinc ion binding free energy
2	0	-443
3	0	-438
4	0	-433
5	0	-432
6	0	-428
6	5	-429
6	10	-432
6	15	-434

### 3.2.2 Radial distribution functions

Radial distribution functions between  $\text{Zn}^{2+}$  and water oxygen and methanol oxygen and methyl groups were calculated using VMD 1.9.1. [18]. Some are shown below in Figure 5. The other radial distribution functions can be found in Appendix C.1.

From the radial distribution functions, we see that the locations of the peaks do not move with changing solvent methanol composition or coordination shell methanol composition, but the heights of the peaks change. This shows that effect of the methanol on the general structure of the inner shell is minimal, but it does push the outer shell further away from the zinc. This is what most likely explains the trend observed in the solvation free energies above: adding more methanol to the inner shell decreases the stability of the system by virtue of its size. The plots also show that a radius of 3.5 Å for the outer shell is a reasonable choice.



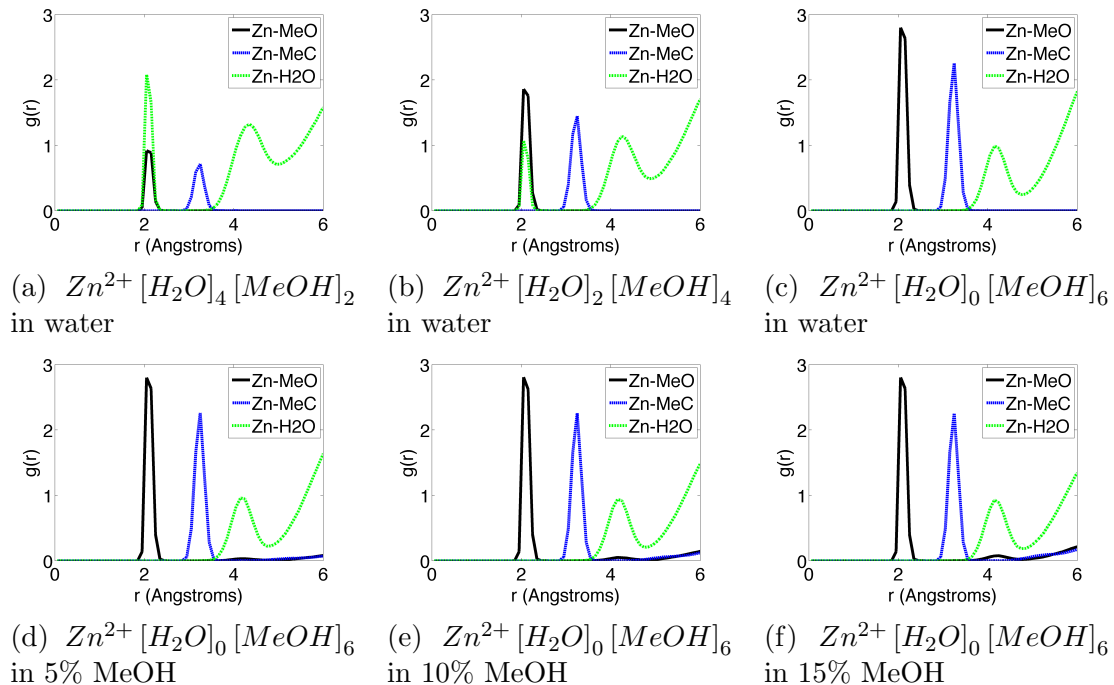


Figure 5: Radial distribution functions

### 3.2.3 Occupancy probabilities

Occupancy probabilities were determined using a VMD Tcl script (See Appendix B.2). For the quasi-chemical approximation, a specific number of each kind of atom in the inner shell is assumed. To verify that this assumption is reasonable, the probability that the area around the ion is occupied by a certain number of waters and methanols was calculated. Table 4 shows the probabilities that an *incorrect* number of atoms each non-hydrogen type were observed. Correctness was defined as the following: for simulations with  $n$  MeOH in the coordinated to the ion, there should be  $n$  methanol oxygens,  $n$  methanol methyl groups, and  $6 - n$  water oxygens within the  $3.5 \text{ \AA}$  boundary.

From the small probabilities in Table 4, we see that the assumption that the shell consists of  $n$  methanols and  $6 - n$  waters is reasonable.

Table 4: Probabilities that incorrect numbers of each atom type are within 3.5 Å of  $\text{Zn}^{2+}$

$n = \text{MeOH}$	MeOH mol%	$P(\text{Me}\mathbf{O}H \neq n)$	$P(\mathbf{M}eOH \neq n)$	$P(\mathbf{O}H_2 \neq 6 - n)$
2	0	0	$9.1 \times 10^{-3}$	$2.2 \times 10^{-2}$
3	0	0	$1.4 \times 10^{-2}$	$1.6 \times 10^{-2}$
4	0	0	$1.9 \times 10^{-2}$	$1.2 \times 10^{-2}$
5	0	0	$2.6 \times 10^{-2}$	$9.9 \times 10^{-3}$
6	0	0	$3.2 \times 10^{-2}$	$7.4 \times 10^{-3}$
6	5	$6.7 \times 10^{-5}$	$3.2 \times 10^{-2}$	$6.8 \times 10^{-3}$
6	10	$2.3 \times 10^{-4}$	$3.3 \times 10^{-2}$	$7.0 \times 10^{-3}$
6	15	$2.4 \times 10^{-3}$	$3.2 \times 10^{-2}$	$6.9 \times 10^{-3}$

These are the probabilities that the specified number of the centers of the atom type in **bold** is within 3.5Å of the ion.

### 3.2.4 Quasi-chemical calculations of free energies

Based on the observation that the zinc ion bound the nearest six molecules tightly, and that it always exhibited a hexacoordinated geometry, QM calculations of the  $\text{Zn}^{2+}$  ion with different coordination shells containing  $i$  waters and  $6 - i$  methanols for  $i$  ranging from 0 to 6 were performed, and Equation 2.4 was used to determine the free energies for all the coordination states. It was determined that there were several isomers of some solvation shells. An example of this is shown in Figure 6

QM optimizations of the geometries from Figure 6 revealed that the energy differences were negligible ( $< 0.1 \frac{\text{kcal}}{\text{mol}}$ ), hence only one isomer was used.

A table (Table 5) of the solvation free energies in water of each coordination state (neglecting the probability term in Equation 2.4) and their contributions is shown below.

Also, we assume ideal solutions to calculate the standard state correction ( $-kT \ln \rho^6$ ) (see Section 2.1.4). However, since the term is not very large, such an approximation

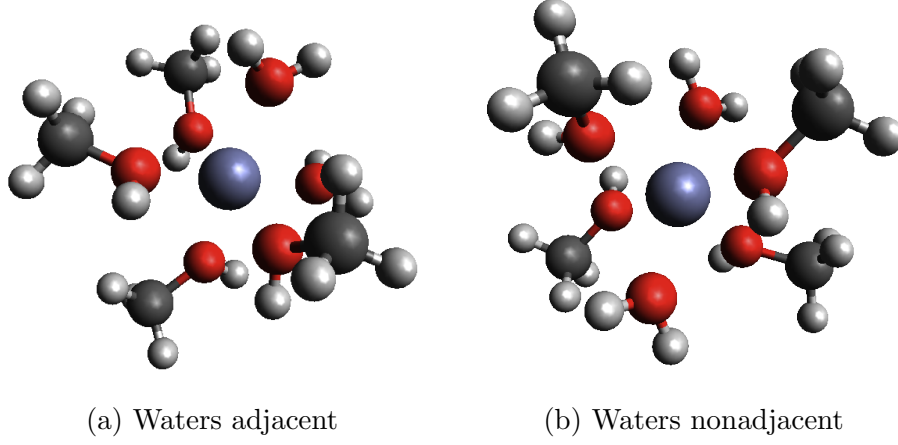


Figure 6: Two isomers of a  $\text{Zn}^{2+}$  ion coordinated with 4 MeOH and 2  $\text{H}_2\text{O}$ .

Table 5: Quasi-chemical calculation of  $\text{Zn}^{2+}$  solvation free energies with different coordination numbers

Units in $\left(\frac{\text{kcal}}{\text{mol}}\right)$	$kT \ln K_{n,m}^{(0)}$	$-kT \ln \rho^6$	$\mu_{XL_1nL_2m}^{ex}$	$n\mu_{L_1}^{ex} + m\mu_{L_2}^{ex}$	$\mu_X^{ex}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_6 [\text{MeOH}]_0$	-283	-25.6	-203	-49	-462
$\text{Zn}^{2+} [\text{H}_2\text{O}]_5 [\text{MeOH}]_1$	-285	-25.3	-195	-46	-459
$\text{Zn}^{2+} [\text{H}_2\text{O}]_4 [\text{MeOH}]_2$	-287	-24.9	-187	-43	-455
$\text{Zn}^{2+} [\text{H}_2\text{O}]_3 [\text{MeOH}]_3$	-289	-24.5	-180	-41	-453
$\text{Zn}^{2+} [\text{H}_2\text{O}]_2 [\text{MeOH}]_4$	-291	-24.0	-174	-39	-451
$\text{Zn}^{2+} [\text{H}_2\text{O}]_1 [\text{MeOH}]_5$	-292	-23.5	-168	-36	-447
$\text{Zn}^{2+} [\text{H}_2\text{O}]_0 [\text{MeOH}]_6$	-294	-22.8	-162	-34	-445

will not affect the calculation much.

To account for the different solvents, the dielectric constant was adjusted using the methodology in [20]. Table 6 shows the solvation free energies in various mixtures.

Table 6: Quasi-chemical calculation of  $\text{Zn}^{2+}$  solvation free energies in water/methanol mixtures

MeOH mol%	0%		15%		100%	
Dielectric Constant	78.4		65		33	
Units in $\left(\frac{\text{kcal}}{\text{mol}}\right)$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu_{L_{1n}L_{2n}}^{ex}$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu_{L_{1n}L_{2n}}^{ex}$	$\mu_{XL_{1n}L_{2m}}^{ex}$	$\mu_{L_{1n}L_{2n}}^{ex}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_6 [\text{MeOH}]_0$	-203	-49	-202	-48	-199	-47
$\text{Zn}^{2+} [\text{H}_2\text{O}]_5 [\text{MeOH}]_1$	-195	-46	-194	-46	-191	-45
$\text{Zn}^{2+} [\text{H}_2\text{O}]_4 [\text{MeOH}]_2$	-187	-44	-186	-44	-183	-42
$\text{Zn}^{2+} [\text{H}_2\text{O}]_3 [\text{MeOH}]_3$	-180	-41	-179	-41	-176	-40
$\text{Zn}^{2+} [\text{H}_2\text{O}]_2 [\text{MeOH}]_4$	-174	-39	-174	-39	-171	-38
$\text{Zn}^{2+} [\text{H}_2\text{O}]_1 [\text{MeOH}]_5$	-168	-36	-167	-36	-165	-35
$\text{Zn}^{2+} [\text{H}_2\text{O}]_0 [\text{MeOH}]_6$	-162	-34	-162	-34	-159	-33

We see that there are no large differences in free energies from this method along the range of MeOH mol% studied. The main differences in free energy arise from the  $\mu_{XL_{1n}L_{2m}}^{ex}$  term. From this calculation, it appears that the water-coordinated state is most favorable even in pure methanol.

Since no exchanges were observed between atoms in the inner shell and atoms outside the inner shell in the simulations, it was not possible to determine the relative probabilities of each coordination state from the trajectories. However, based on the free energy differences of each coordination state, it is possible to determine the relative probabilities: for each coordination state,  $\mu_X^{ex}$  will be the same, with the differences between the free energies accounted for with the  $-kT \ln p_X(0)$  term. Solving for the relative probability in this manner, we obtain the probabilities of each configuration shown in Table 7.

Table 7: Probabilities of observing different coordination states of  $\text{Zn}^{2+}$

Units in $\left(\frac{\text{kcal}}{\text{mol}}\right)$	$\mu_X^{ex}$	$p_X(n, m)$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_6 [\text{MeOH}]_0$	-462	0.997
$\text{Zn}^{2+} [\text{H}_2\text{O}]_5 [\text{MeOH}]_1$	-459	$2.33 \times 10^{-3}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_4 [\text{MeOH}]_2$	-455	$7.02 \times 10^{-6}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_3 [\text{MeOH}]_3$	-453	$7.14 \times 10^{-8}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_2 [\text{MeOH}]_4$	-451	$3.09 \times 10^{-9}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_1 [\text{MeOH}]_5$	-447	$1.03 \times 10^{-11}$
$\text{Zn}^{2+} [\text{H}_2\text{O}]_0 [\text{MeOH}]_6$	-445	$1.35 \times 10^{-13}$

We see that at equilibrium,  $\text{Zn}^{2+}$  would be coordinated to six waters. Since the free energies in differing solvent do not change by much (see Table 6), we conclude that a six water coordinated  $\text{Zn}^{2+}$  ion will be the most stable in any water/methanol solvent.

### 3.2.5 Charge transfer on $\text{Zn}^{2+}$ ions in QM calculations

The charges on the  $\text{Zn}^{2+}$  ion from the different QM calculations were computed using electrostatic fitting (see Table 8).

From these results, we can see that charge transfer plays a significant role in terms of quantum effects in this system. This verifies the need to treat the core with an electronic structure method.

## 3.3 TFIIIA zinc finger motif

### 3.3.1 AMBER FF09 simulations

MD simulations were also performed for the zinc finger motif present in TFIIIA. The zinc finger motif was taken from chain A of the TFIIIA, residues 42-71. These residues

Table 8: Charge transfer off of  $\text{Zn}^{2+}$  ion

Number of Methanols	Charge on $\text{Zn}^{2+}(e)$
0	2.09
1	1.92
2	1.75
3	1.60
4	1.34
5	1.09
6	0.80

P-F-P-**C**-K-E-E-G-**C**-E-K-G-F-T-S-L-H-H-L-T-R-**H**-S-L-T-**H**-T-G-E-K

Figure 7: Sequence of peptide used. Zinc ligands are in bold.

were chosen as this peptide’s properties had been characterized by early studies [4]. The sequence of the peptide is shown in Figure 7.

The NMR structure of the protein with the zinc binding site is shown in Figure 8. Note that the zinc ion appears to be tetrahedrally coordinated by the four amino acids.

The motif was solvated in a  $48\text{\AA} \times 48\text{\AA} \times 54\text{\AA}$  water box, minimized for 10000 steps, and heated to 298  $K$  over 50 ps. Ten nanosecond NPT production runs were performed and were used for trajectory analysis. The CHARMM27 force field was unable to produce a stable structure with the zinc ion within the binding site. However, the AMBER FF09 force field was able to do so. Interaction energies between the  $\text{Zn}^{2+}$  ion and all other atoms were obtained from the trajectory. The interaction energies were normally distributed (see Figure 9). The solvation free energy was calculated using Equation 2.2, and the components are tabulated in Table 9.

In the equilibrated structure, the  $\text{Zn}^{2+}$  ion was coordinated to two waters in addition to the four protein ligands as seen in the NMR structure (see Figure 10). In

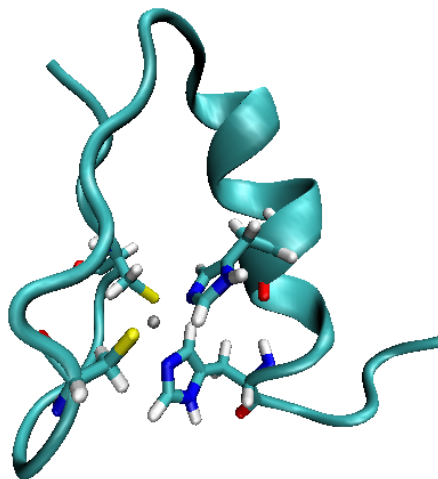


Figure 8: TFIIIA Zinc finger motif NMR structure with binding site. Grey ball is zinc, yellow is sulfur. The cysteine side chains are on the right, the histidines are on the left.

Table 9: Components of zinc finger solvation free energy

$\langle \epsilon \rangle \left( \frac{kcal}{mol} \right)$	$\frac{\beta \sigma^2}{2} \left( \frac{kcal}{mol} \right)$	$\mu_X^{ex} \left( \frac{kcal}{mol} \right)$
-652	130	-522

order to reproduce the NMR structure, other methods were used to reparameterize the inner core. From the literature, it was determined that the cause of the extra waters in the binding site was inadequate consideration of quantum effects such as charge transfer and polarization [21].

### 3.3.2 Non-QM methods for accounting for quantum effects

To account for charge transfer, the charges on the  $Zn^{2+}$  ion and the surrounding ligands were modified by hand using the charges from Li et al [21], who used the electron densities from a QM optimization calculation to determine the charge transfer. This method did not, however, exclude the waters from entering the zinc finger. Using the CHARMM 27 force field with this parameterization resulted in a stable protein, but

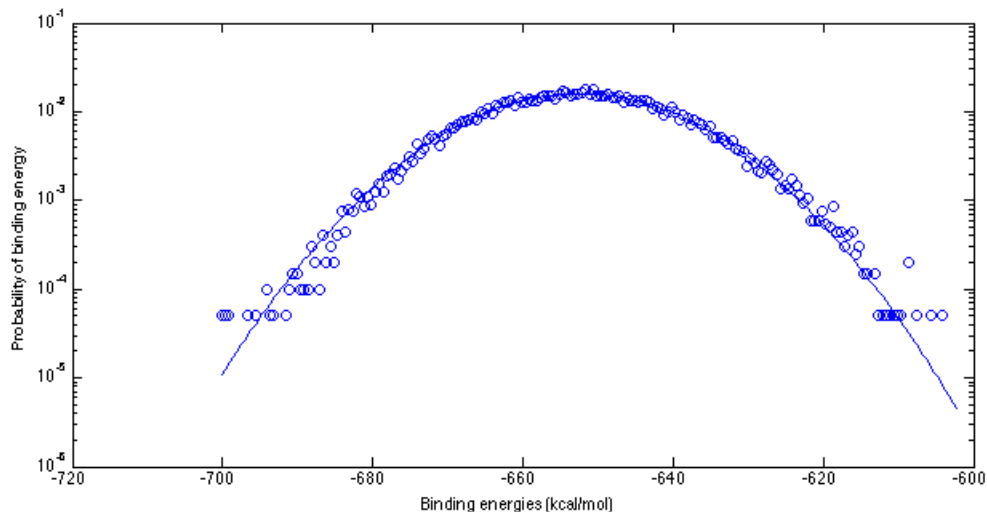


Figure 9: Zinc finger  $\text{Zn}^{2+}$  interaction energy distribution and gaussian fit.

with the waters in the binding site as shown in Figure 10.

Simulations were also performed using the cationic dummy atom model [22], which uses four charged "dummy atoms" attached to the zinc ion by springs in order to approximate polarization effects. This model was able to successfully predict the structure, but since it constrained the ligands, the vibrational modes would be affected. It was decided to explore chemical and quasi-chemical approaches for determining the free energies.

### 3.3.3 QM/MM calculations

QM/MM calculations were performed on the zinc finger to determine an optimized QM geometry for the core as well as an optimized MM geometry for the rest of the protein. The side chains of the protein and the zinc ion were treated with DFT using the LANL08DZ basis set, which is optimized for transition metals. The B3LYP hybrid functional was used. The rest of the atoms were treated using the AMBER FF09 force field. QM/MM dynamics at the time lengths required for determination of the free energies were not feasible. QM/MM methods were used to optimize geometries for the zinc finger core in order to have accurate geometries for usage with the quasi-chemical



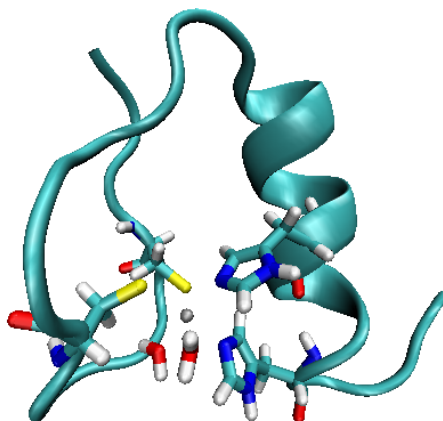


Figure 10: Zinc finger equilibrated structure. Note the two water molecules in the binding site.

method.

## 4 Discussion

### 4.1 Ions in water

#### 4.1.1 MD simulations

From the results in Table 1, we conclude that these simulations do indeed contain good measures of the binding free energy of the  $\text{Zn}^{2+}$  ion to water. While there are errors on the order of tens of  $\frac{\text{kcal}}{\text{mol}}$ , the trends are the same. However, since we are extending these results to measuring stability changes in mutations of proteins, a more accurate method may be necessary.

#### 4.1.2 Quasi-chemical calculation of $\text{Zn}^{2+}$ hydration free energy

The hydration free energies calculated using the quasi-chemical method agreed very well with those of Asthigiri et al [8], which demonstrates that the procedure used

was accurate enough. The differences are mainly due to the usage of a larger basis set and a different method of solving the Poisson-Boltzman equation.

## 4.2 Zinc ion in water and methanol

### 4.2.1 Inner-shell stability

The zinc ion binds its coordinating ligands very tightly. Because of this, any exchanges were not able to be modeled, as the initial configuration of the zinc coordination shell did not change throughout the simulation. Increasing temperature to increase the fluctuations of the atoms was unsuccessful at dislodging any of the coordinating ligands. This effect can also be seen in the relatively sharp peaks of the radial distribution functions (see C.1). Because of this, it was impossible to use simulations to determine the most stable coordination state, so it was done using solvation free energies.

### 4.2.2 Effect of coordination shell composition

From the quasi-chemical calculations of the free energy of solvation with different coordination states (Table 5, the largest quantity in the calculation of the solvation free energy is the equilibrium constant term  $-kT \ln K(0)_{n,m}$ . It decreases with increasing methanol around the zinc finger. Such an effect could be due to the fact that the larger system (more atoms) allows the electrons to delocalize more than with water. The outer shell contribution increases greatly with increasing methanols, and it dominates the differences in free energy. This is most likely due to the increasing size of the complex, which can be seen from the radial distribution functions C.1. The decreasing second-shell water peak and increasing third-shell water peaks are due to more of the water being pushed away from the ion. Since it takes more work to take a larger charged sphere into an electric field, it is reasonable that increasing the size would destabilize the system. We also see this pattern in the MD simulations (see

Table 3), as the cluster solvation free energies also increase by a similar amount (2-4  $\frac{\text{kcal}}{\text{mol}}$ ). Overall, the results suggest that the aqueous coordinated state is the most stable.

There is no experimental data regarding the solvation free energy of the zinc ions in water/methanol mixtures, so it is not possible to compare the simulation data to actual data. However, as the MD simulations and QC calculations agree in terms of the relative differences in free energy between the coordination states, these may still be good estimates of the actual values.

### 4.2.3 Effect of solvent composition

One concern with the simulations is the different trends with regards to changing the solvent. In the MD simulations (Table 3), it appears that increasing methanol in the solvent actually tends to stabilize the cluster by a significant amount. However, the opposite appears to be true concerning the QC calculations (Table 6). Additional methanol in the solvent (lowering the dielectric constant) is unfavorable, but the effect is not very large. These discrepancies could be due to the nature of the approximations made. In the QC calculations, the outer shell is treated as a purely electrostatic entity. However, along the edges of the cluster, the van der Waals forces could be playing an important role. Because of this, a more advanced quasi-chemical approximation with a higher-level representation of the outer shell may be necessary.

## 4.3 Zinc fingers

While this work did not truly explore the stability of zinc fingers, some insight was still gained into methods of modeling zinc fingers. Firstly, classical methods are unable to reproduce the tetracoordinated geometry of the zinc finger. This may be due to the nature of the parameterization of the zinc ion in force fields, as in solution, the zinc ion is indeed hexacoordinated.

### 4.3.1 Application of zinc ion in water/methanol mixtures to zinc finger thermodynamics

Two methods of applying the quasi-chemical method to zinc fingers arise. Firstly, one can consider the entire protein as the ligand in the inner shell. Secondly, one can consider the sidechains of the protein ligands as the inner shell, and the rest of the protein and the water as the outer shell. Both methods have challenges. In the first method, modeling the entire protein using QM would be unfeasible. Also, in order to use the quasi-chemical method, we need to know the solvation free energy of the protein without the zinc ion (see Equation 2.4). Since we do not know the conformation of the protein without the ion, it may be very difficult to estimate accurately. However, if we consider relative binding free energies of different ions instead, we can approximate the relative reaction free energy changes in the protein-zinc system by free energy changes in the binding site. The term with the protein without the ion cancels out. Thus, this method can be used to determine relative binding free energies.

For the second method, since the quasi-chemical model treats the outer shell electrostatically using the dielectric constant, a dielectric constant for the zinc finger protein is required. This can be calculated from MD trajectories. However, if we mutate only one residue, it may be difficult to have a significant effect on the dielectric constant. As can be seen from Table 6, small dielectric constant changes do not affect the solvation free energy much in that approximation. Also, in a protein, van der Waals and bonded interactions of the sidechains in the inner shell with the outer shell are more important.

To overcome these limitations, the outer shell component of the solvation free energy can also be approximated using the inverse potential distribution theorem and MD with the method described in Section 2.2.3. Several factors need to be addressed before such a calculation can take place. Firstly, the bonded interactions need to be

considered. One of the principle difficulties in QM/MM calculations, another method seeking to bridge quantum and classical simulations, is in the coupling of the two forms of simulation. Methodologies from QM/MM may also be applicable to QC calculations. Secondly, a method of simulating the protein with MD that gives good estimates of the outer-shell free energies is required. Several methods exist, but their effects on the calculation of free energies has yet to be considered. Thirdly, an accurate estimate of the geometry of the inner shell is necessary. This was performed using QM/MM geometry optimizations to determine an accurate inner shell geometry that also considered the overall conformation of the protein.

## 5 Conclusions

Several methods can be used to estimate the free energy of hydration of ions in solution. Two of these are quasi-chemical theory and the inverse potential distribution theorem. Using the IPDT with MD simulation data yields results accurate to within tens of  $\frac{kcal}{mol}$ . Quasi-chemical theory uses electronic structures to determine the formation and solvation free energies of a certain complex. The formulation of the IPDT lends itself naturally to mixtures in solutions.

QC theory was also expanded to include different ligands coordinating the species of interest. A derivation can be found in section 2.1.4. The solvation free energy of different coordination states of the  $Zn^{2+}$  ion was found to follow two opposite trends. Firstly, the free energy of formation of the inner shell was found to decrease with increasing methanols in the coordination shell. This may be due to the fact that a larger system allows for better electron delocalization, stabilizing the chemical equilibrium. Secondly, the free energy contribution of solvation of the inner shell cluster was found to increase with increasing methanols in the coordination shell. This may be due to the fact that a larger system also requires more work to solvate.

This was supported by MD simulations. The second trend was more dominant in the zinc-methanol-water system, and the most favorable hexacoordinated state was the zinc ion with six water molecules.

Extending QC theory to mixtures of solvents reduces to changing the dielectric constant of the solvent and using that to solvate the inner shell cluster. However, this yielded discrepancies with the MD simulations. These discrepancies require further investigation. It was observed, however, that the dielectric constant made little impact on the free energies in the case of water and methanol solutions. This may not be true for mixtures of fluids with more disparate dielectric constants.

From these observations, in order to adapt these methods for determining the binding free energies of the  $\text{Zn}^{2+}$  ions in zinc fingers, it will be beneficial to use one of two methods. First, the free energy change for different ions in the protein can be measured instead using a quasi-chemical model where the entire protein is in the inner shell as the ion ligand. Secondly, a combined method could be used. In this quasi-chemical framework, the “inner shell” would be considered using QM calculations as before. However, the “outer shell” would be treated using MD simulations and the IPDT to determine solvation free energies of the cluster. Some theoretical issues in computing the binding free energies include computing the core structure accurately, simulating the protein accurately using MD, and the treatment of bonds and van der Waals forces. Several approaches exist for the first and second challenges. The third problem has similarities with problems in calculating energies using QM/MM methods and similar approaches can be used. The ability to accurately compute binding free energies of such proteins will allow for the better design of stable synthetic zinc finger therapies for many genetic and viral disorders.

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## A Sample Input Files

### A.1 Gaussian Input Files

#### A.1.1 Geometry Optimization

```
%chk=ZnMeOH_1MeOH.2.chk
%nproc=8
%mem=8GB
# B3LYP/6-31+G(d,p) Opt=(MaxCycles=3000) SCF=Tight

ZnMeOH_1MeOH initial optimization

2 1
Zn
O      1      2.12893
H      2      0.96755      1      126.17828
H      2      0.96757      1      125.75120      3      170.40655
O      1      2.13616      2      87.12158      3      94.83202
H      5      0.96761      1      125.02553      2      359.41570
H      5      0.96745      1      127.44986      2      180.60039
O      3      4.91606      1      7.01409      2      166.75975
H      8      0.96777      1      125.97754      2      273.69230
H      8      0.96776      1      126.28971      2      84.80468
C      1      3.27698      2      77.67952      3      274.51543
O      11      1.46857      1      27.07727      2      179.43446
H      12      0.96628      11      109.55118      1      179.32941
H      11      1.08519      1      79.64376      2      0.77357
H      11      1.08816      1      120.94433      2      108.22552
H      11      1.08818      1      119.82954      2      253.25482
H      1      2.81424      2      88.72717      3      167.08164
O      17      0.96758      1      37.82510      2      92.74253
H      18      0.96749      17      107.47534      1      178.20228
```

O	1	2.13326	2	89.99628	3	5.86169
H	20	0.96751	1	126.00081	2	265.86735
H	20	0.96756	1	126.52056	2	85.96788

*%chk=ZnMeOH\_1MeOH.2.chk*

*%nproc=8*

*%mem=8GB*

# B3LYP/6-311+G(d,p) Opt=(MaxCycles=3000) SCF=Tight Geom=check guess=read

ZnMeOH\_1MeOH opt1 optimization

2 1

*%chk=ZnMeOH\_1MeOH.2.chk*

*%nproc=8*

*%mem=8GB*

# B3LYP/6-311++G(2d,p) Opt=(VeryTight,MaxCycles=3000) SCF=Tight Geom=check guess=read

ZnMeOH\_1MeOH opt2 optimization

2 1

## A.1.2 Frequency and Population Analysis

*%chk=ZnMeOH\_1MeOH.2.chk*

*%nproc=8*

*%mem=8GB*

# Freq Pop=(ChelpG, ReadRadii) b3lyp/6-311++g(2d,p) geom=checkpoint guess=read

ZnMeOH\_1MeOH frequency and population analysis

2 1

Zn 2.2

C 2.096

O 1.576

H 1.172

## A.2 NAMD Parameters

### A.2.1 CHARMM27

Standard CHARMM27 parameters were used, with the CYM residue using the following parameterization:

```
RESI CYM          -1.00
! Thiolate form
! Foloppe, N., J. Sagemark, K. Nordstrand, K.D. Berndt, and L. Nilsson
! (2001). J. Mol. Biol. 310:449-470.
! Atom types and charges transfered from methythiolate
GROUP
ATOM N    NH1    -0.47  !      |
ATOM HN   H      0.31  !  HN-N
ATOM CA   CT1    0.07  !      |  HB1
ATOM HA   HB     0.09  !      |  |      -
GROUP          !  HA-CA-CB-SG    (thiolate)
ATOM CB   CS    -0.38  !      |  |

ATOM HB1  HA     0.09  !      |  HB2
ATOM HB2  HA     0.09  !  O=C
ATOM SG   SS    -0.80  !      |
GROUP
ATOM C    C      0.51
ATOM O    O     -0.51
BOND CB CA  SG CB  N HN  N  CA
BOND O  C    C  CA  C +N  CA HA  CB HB1  CB HB2
IMPR N -C CA HN  C CA +N O
DONOR HN N
ACCEPTOR O C
IC -C  CA  *N  HN    1.3479 123.9300 180.0000 114.7700 0.9982
IC -C  N   CA  C     1.3479 123.9300 180.0000 105.8900 1.5202
IC N   CA  C   +N    1.4533 105.8900 180.0000 118.3000 1.3498
IC +N  CA  *C  O     1.3498 118.3000 180.0000 120.5900 1.2306
IC CA  C   +N  +CA   1.5202 118.3000 180.0000 124.5000 1.4548
IC N   C   *CA  CB   1.4533 105.8900 121.7900 111.9800 1.5584
IC N   C   *CA  HA   1.4533 105.8900 -116.3400 107.7100 1.0837
IC N   CA  CB  SG    1.4533 111.5600 180.0000 113.8700 1.8359
IC SG  CA  *CB  HB1  1.8359 113.8700 119.9100 107.2400 1.1134
IC SG  CA  *CB  HB2  1.8359 113.8700 -125.3200 109.8200 1.1124
```

## A.2.2 AMBER FF09

Standard FF09 parameters were used.

## A.2.3 OPLS-ua

The topology file

\* DK's & HP's TOP

\*

	22	1	
MASS	1 HT	1.00800 H !	TIPS3P WATER HYDROGEN
MASS	2 OT	15.99940 O !	TIPS3P WATER OXYGEN
MASS	3 OH	15.99940 O !	Hydronium oxygen
MASS	4 HH	1.00800 H !	Hydronium hydrogen
MASS	5 HC	1.00800 H !	Hydrogen to carbon
MASS	6 HN	1.00800 H !	
MASS	7 C	12.00000 C	
MASS	8 N	14.00700 N	
MASS	9 HQ	1.00800 H	
MASS	10 OQ	16.00000 O	
MASS	11 BE	9.00000 Be	
MASS	12 HS	1.00800 H !	SPCE WATER HYDROGEN
MASS	13 OS	15.99940 O !	TIPS3P WATER OXYGEN
MASS	14 Kr	83.00000 Kr !	Check mass number
MASS	15 Ne	20.00000 Ne !	Check mass number
MASS	16 KG	83.00000 KG !	Krypton Guissani
MASS	17 NG	20.00000 NG !	Neon Guissani
MASS	18 HF	1.00800 H !	Formate hydrogen
MASS	19 CF	12.00000 C !	Formate Carbon
MASS	20 OF	15.99940 O !	Formate Oxygen
MASS	21 P	31.0000 P !	Phosphorus
MASS	22 CH4	16.0320 C !	Methane United atom check methane mass
MASS	23 CH3	15.0240 C !	Methyl
MASS	24 OA	15.99940 O !	Alcohol oxygen
MASS	25 HA	1.00800 H !	Alcohol hydrogen
MASS	26 CHE	15.0240 C !	Methyl in Ethane
MASS	27 CHK	15.0240 C !	Methyl KBFF for Methanol JPCB 109 2005 15080–15086
MASS	28 OAK	15.99940 O !	Alcohol oxygen KBFF
MASS	28 HAK	1.00800 H !	Alcohol hydrogen KBFF
MASS	29 NPC	12.0000 C !	Neopentane center carbon

MASS 30 NPX 15.99940 C ! Neopentane methyl groups  
 MASS 196 ZN 65.370000 ZN ! zinc (II) cation

AUTO ANGLES DIHE

RESI TIP3 0.000

GROUP

ATOM OH2 OT -0.834

ATOM H1 HT 0.417

ATOM H2 HT 0.417

BOND OH2 H1 OH2 H2

ANGLE H1 OH2 H2

ACCEPTOR OH2

PATCHING FIRS NONE LAST NONE

RESI SPCE 0.000

GROUP

ATOM OH2 OS -0.8476

ATOM H1 HS 0.4238

ATOM H2 HS 0.4238

BOND OH2 H1 OH2 H2 H1 H2

ANGLE H1 OH2 H2

ACCEPTOR OH2

PATCHING FIRS NONE LAST NONE

RESI O2M -1.000

GROUP

ATOM OM1 OS -0.5000

ATOM OM2 OS -0.5000

ACCEPTOR OM1

ACCEPTOR OM2

PATCHING FIRST NONE LAST NONE

RESI Kryp 0.000

GROUP

ATOM Kr Kr 0.000

PATCHING FIRST NONE LAST NONE

RESI MET 0.000

GROUP

ATOM CH4 CH4 0.000

PATCHING FIRST NONE LAST NONE

RESI MEOH 0.000

GROUP

ATOM C CH3 0.265

ATOM O OA -0.700

ATOM H HA 0.435

BOND C O O H

ANGLE C O H

DONOR H O

ACCEPTOR O C

PATCHING FIRST NONE LAST NONE

RESI MOHK 0.000

GROUP

ATOM C CHK 0.300

ATOM O OAK -0.820

ATOM H HAK 0.52

BOND C O O H C H

ANGLE C O H

DONOR H O

ACCEPTOR O C

PATCHING FIRST NONE LAST NONE

RESI ETH 0.000

GROUP

ATOM C1 CHE 0.000

ATOM C2 CHE 0.000

BOND C1 C2

PATCHING FIRST NONE LAST NONE

RESI NEOP 0.000

GROUP

ATOM CC NPC 0.000

ATOM C1 NPX 0.000

ATOM C2 NPX 0.000

ATOM C3 NPX 0.000

ATOM C4 NPX 0.000

BOND CC C1 CC C2

BOND CC C3 CC C4

ANGLE C1 CC C2 C2 CC C3



ANGLE C3 CC C4 C4 CC C1  
 ANGLE C1 CC C3 C2 CC C4  
 PATCHING FIRST NONE LAST NONE

RESI KRYG 0.000  
 GROUP  
 ATOM KG KG 0.000  
 PATCHING FIRST NONE LAST NONE

RESI NEO 0.000  
 GROUP  
 ATOM Ne Ne 0.000  
 PATCHING FIRST NONE LAST NONE

RESI NEG 0.000  
 GROUP  
 ATOM NG NG 0.000  
 PATCHING FIRST NONE LAST NONE

RESI 3PIT 0.000  
 GROUP  
 ATOM OH2 OT 0.000  
 ATOM H1 HT 0.000  
 ATOM H2 HT 0.000  
 BOND OH2 H1 OH2 H2 H1 H2  
 ANGLE H1 OH2 H2  
 ACCEPTOR OH2  
 PATCHING FIRST NONE LAST NONE

RESI H3O 1.000  
 GROUP  
 ATOM OH2 OH -0.521  
 ATOM H1 HH 0.507  
 ATOM H2 HH 0.507  
 ATOM H3 HH 0.507  
 ! BOND OH2 H1 OH2 H2 OH2 H3  
 PATCHING FIRST NONE LAST NONE

RESI O3H 0.000  
 GROUP  
 ATOM OH2 OH 0.000

ATOM	H1	HH	0.000
ATOM	H2	HH	0.000
ATOM	H3	HH	0.000
BOND	OH2	H1 OH2 H2 OH2 H3	
PATCHING	FIRST	NONE	LAST NONE

RESI	OH3	0.000	
GROUP			
ATOM	O1	OS 0.000	
ATOM	O2	OS 0.000	
ATOM	O3	OS 0.000	
ATOM	O4	OS 0.000	
ATOM	H5	HS 0.000	
ATOM	H6	HS 0.000	
ATOM	H7	HS 0.000	
ATOM	H8	HS 0.000	
ATOM	H9	HS 0.000	
ATOM	H10	HS 0.000	
ATOM	H11	HS 0.000	
PATCHING	FIRST	NONE	LAST NONE

RESI	H5O2	1.000	
GROUP			
ATOM	H1	HQ 0.505	
ATOM	O2	OQ -0.734	
ATOM	O3	OQ -0.730	
ATOM	H4	HQ 0.474	
ATOM	H5	HQ 0.505	
ATOM	H6	HQ 0.475	
ATOM	H7	HQ 0.505	
!	BOND	H1 O2 H1 O3	
!	BOND	O2 H6 O2 H7	
!	BOND	O3 H4 O3 H5	
PATCHING	FIRST	NONE	LAST NONE

RESI	2O5H	0.000
GROUP		
ATOM	H1	HQ 0.000
ATOM	O2	OQ 0.000
ATOM	O3	OQ 0.000

ATOM	H4	HQ	0.000
ATOM	H5	HQ	0.000
ATOM	H6	HQ	0.000
ATOM	H7	HQ	0.000
! BOND H1 O2 H1 O3			
! BOND O2 H6 O2 H7			
! BOND O3 H4 O3 H5			
PATCHING FIRST NONE LAST NONE			

RESI	IMD		0.000
GROUP			
ATOM	N1	N	-0.090
ATOM	C2	C	0.232
ATOM	N3	N	-0.716
ATOM	C4	C	0.217
ATOM	C5	C	-0.375
ATOM	H1	HN	0.318
ATOM	H2	HC	0.102
ATOM	H4	HC	0.082
ATOM	H5	HC	0.230
PATCHING FIRST NONE LAST NONE			

RESI	DMI		0.000
GROUP			
ATOM	N1	N	0.000
ATOM	C2	C	0.000
ATOM	N3	N	0.000
ATOM	C4	C	0.000
ATOM	C5	C	0.000
ATOM	H1	HN	0.000
ATOM	H2	HC	0.000
ATOM	H4	HC	0.000
ATOM	H5	HC	0.000
PATCHING FIRST NONE LAST NONE			

RESI	IMP		1.000
GROUP			
ATOM	N1	N	-0.115
ATOM	C2	C	0.011
ATOM	N3	N	-0.123
ATOM	C4	C	-0.140

ATOM	C5	C	-0.122
ATOM	H1	HN	0.399
ATOM	H2	HC	0.230
ATOM	H3	HN	0.403
ATOM	H4	HC	0.232
ATOM	H5	HC	0.225
PATCHING FIRST NONE LAST NONE			

RESI	PMI		0.000
GROUP			
ATOM	N1	N	0.000
ATOM	C2	C	0.000
ATOM	N3	N	0.000
ATOM	C4	C	0.000
ATOM	C5	C	0.000
ATOM	H1	HN	0.000
ATOM	H2	HC	0.000
ATOM	H3	HN	0.000
ATOM	H4	HC	0.000
ATOM	H5	HC	0.000
PATCHING FIRST NONE LAST NONE			

RESI	BER		2.000
GROUP			
ATOM	BE1	BE	2.000
PATCHING FIRST NONE LAST NONE			

RESI	BE4		2.000
GROUP			
ATOM	BE1	BE	1.664
ATOM	O2	OQ	-1.093
ATOM	O3	OQ	-1.093
ATOM	O4	OQ	-1.097
ATOM	O5	OQ	-1.097
ATOM	H6	HQ	0.589
ATOM	H7	HQ	0.591
ATOM	H8	HQ	0.590
ATOM	H9	HQ	0.588
ATOM	H10	HQ	0.589
ATOM	H11	HQ	0.591

ATOM	H12	HQ	0.590
ATOM	H13	HQ	0.588
PATCHING FIRST NONE LAST NONE			

RESI	FOR		-1.000
ATOM	H1	HF	-0.100
ATOM	C2	CF	0.620
ATOM	O3	OF	-0.760
ATOM	O4	OF	-0.760
PATCHING FIRST NONE LAST NONE			

RESI	BEO		0.000
GROUP			
ATOM	O1	OF	-0.659097
ATOM	C1	CF	0.498766
ATOM	O2	OF	-0.393698
ATOM	C2	CF	0.484823
ATOM	O3	OF	-0.390139
ATOM	O4	OF	-0.655186
ATOM	BE1	BE	1.114531
PATCHING FIRST NONE LAST NONE			

RESI	BEP		1.00000
GROUP			
ATOM	BE1	BE	1.70000
ATOM	P	P	1.90000
ATOM	O1	OF	-0.70700
ATOM	O2	OF	-1.30000
ATOM	O3	OF	-0.64400
ATOM	O4	OF	-0.70700
ATOM	H5	HF	0.37900
ATOM	H6	HF	0.37900
PATCHING FIRST NONE LAST NONE			

RESI	PHO		-1.00000
GROUP			
ATOM	P	P	1.36617
ATOM	O1	OF	-0.78008
ATOM	O2	OF	-0.87714
ATOM	O3	OF	-0.70454

```

ATOM  O4   OF      -0.70712
ATOM  H5   HF       0.3526
ATOM  H6   HF       0.35011
PATCHING FIRST NONE LAST NONE

RESI ZN2      2.00 ! Zinc ion , Roland Stote
GROUP
ATOM ZN   ZN   2.00
PATCHING FIRST NONE LAST NONE

END

```

## The parameter file

\* DK's and HP's param file

\*

### BONDS

```

HS   HS      0.000    1.6323 ! SPCE HS-HS distance
HT   HT      0.000    1.5139 ! Required for shake
OT   HT     450.000    0.9572 !
OS   HS     450.000    1.0000 ! SPCE OS-HS distance is different
OQ   HQ     450.000    0.9572 ! Zundel dummy values
OS   OS     450.000    1.3100 ! For superoxide ... largely dummy
OH   HH     450.000    0.9700
N    C      200.000    1.3600
N    HN     450.000    1.0000
C    HC     400.000    1.0800
C    C      200.000    1.3600
OA   HA     553.000    0.9600 ! JPCB 111 2007 4467-4476 &
CH3  OA     386.000    1.4250 ! JACS 106 1984 765-784
CH3  HA      0.000    1.9550 ! Required for shake
CHE  CHE      0.000    1.5300 ! JACS 106 1984 6638-6646
OAK  HAK     553.000    0.9450 ! JPCB 109 2005 15080-15086
CHK  OAK     386.000    1.4300 ! JACS 106 1984 765-784
CHK  HAK      0.000    1.9480 ! For shake
NPC  NPX     268.000    1.5300 ! Supplementary info JACS 118 Page 11225

```

### ANGLES

```

HT   OT   HT      55.000    104.5200
HS   OS   HS      55.000    109.4000 ! SPCE uses tetrahedral

```

HH	OH	HH	55.000	114.0000	
HQ	OQ	HQ	0.000	0.0000	! Zundel dummy values
OQ	HQ	OQ	0.000	0.0000	! Zundel dummy values
CH3	OA	HA	55.000	108.5000	
CHK	OAK	HAK	55.000	108.5000	! same as OPLS
NPX	NPC	NPX	58.35	109.4700	! Fixing at tetrahedral <b>angle</b>

# DIHEDRAL

OQ	HQ	OQ	HQ	0.00	0.000	! Zundel dummy
----	----	----	----	------	-------	----------------

NONBONDED nbxmod 5 atom cdiel shift vatom vdistance vswitch -  
cutnb 14.0 ctofnb 12.0 ctonnb 10.0 **eps** 1.0 e14fac 1.0 wmin 1.5

OT	0.000000	-0.152100	1.768200	
HT	0.000000	-0.046000	0.224500	
OS	0.000000	-0.155394	1.776600	! SPCE Oxygen
HS	0.000000	0.000000	0.000000	! SPCE hydrogen has no sigma
OQ	0.000000	-0.152100	1.768200	
HQ	0.000000	-0.046000	0.224500	
OH	0.000000	-0.152100	1.768200	
HH	0.000000	-0.046000	0.224500	
N	0.000000	-0.017000	1.824000	
C	0.000000	-0.086000	1.908000	
HN	0.000000	-0.015700	0.600000	
HC	0.000000	-0.015000	1.359000	
BE	0.000000	-0.018680	1.143900	! Using Aqvist Li+ parameters
KG	0.000000	-0.335800	2.062500	! Krypton from Guissani/Straatsma
Kr	0.000000	-1.500000	1.829600	! Krypton fit to MP2 results
Ne	0.000000	-0.300000	1.433900	! Neon fit to MP2 results
NG	0.000000	-0.036880	1.703300	! Neon from Guissani/Straatsma
CF	0.000000	-0.070000	2.000000	! Formate carbon
OF	0.000000	-0.120000	1.700000	! Formate oxygen
HF	0.000000	-0.046000	0.224500	! Formate hydrogen
P	0.000000	-0.585000	2.150000	! Phosphorus atom
CH4	0.000000	-0.294000	2.093390	! Jorgensen methane
CH3	0.000000	-0.207000	2.118650	! Methonal (methyl) JPC 90 1986 1276-1284
OA	0.000000	-0.170000	1.722980	! Alcohol oxygen JPC 90 1986 1276-1284
HA	0.000000	0.000000	0.000000	! Alcohol hydrogen
CHE	0.000000	-0.207000	2.118650	! Ethane (methyl) JACS 106 1984 6638-6646
CHK	0.000000	-0.207270	2.103490	! Methonal (methyl) JPC 90 1986 1276-1284
OAK	0.000000	-0.155500	1.791450	! Alcohol oxygen JPC 90 1986 1276-1284

```

HAK      0.000000   -0.021030    0.886750   ! Alcohol hydrogen
NPX      0.000000   -0.145000    2.222470   ! JACS 106 1984 6638-6646
NPC      0.000000   -0.050000    2.132670   ! JACS 106 1984 6638-6646

ZN       0.000000   -0.250000    1.090000   ! ALLOW ION
                        ! RHS March 18, 1990
END

```

## A.3 NAMD Input files

### A.3.1 Ion and Solvent MD

```

#####
## JOB DESCRIPTION                                     ##
#####

# Running simulation for ZnMeOH with 5 mol% MeOH

#####
## ADJUSTABLE PARAMETERS                             ##
#####

set simname      MeOH_15

structure        $simname.psf
coordinates      $simname.pdb
set temperature  298
set outputname   $simname

firsttimestep    0

#####
## SIMULATION PARAMETERS                             ##
#####

# Input
paraTypeCharmm   on
parameters       par.inp
temperature      $temperature

```



```

# Force-Field Parameters
exclude          scaled1-4
1-4scaling       1.0
cutoff           12
switching        on
switchdist       10
pairlistdist     13.5

# Integrator Parameters
timestep         2.0  ;# 1fs/step
rigidBonds       none  ;# needed for 2fs steps
nonbondedFreq    1
fullElectFrequency 2
stepspcycle      10

# Constant Temperature Control
langevin         on    ;# do langevin dynamics
langevinDamping  5     ;# damping coefficient (gamma) of 5/ps
langevinTemp     $temperature
langevinHydrogen off    ;# don't couple langevin bath to hydrogens

# Periodic Boundary Conditions
cellBasisVector1 35    0    0
cellBasisVector2  0    35    0
cellBasisVector3  0     0   35
cellOrigin       12   12   12

wrapAll          on

# Fixed Atoms
#fixedAtoms on
#fixedAtomsFile $simname.pdb
#fixedAtomsCol B
# PME (for full-system periodic electrostatics)
PME              yes
PMEGridSizeX     64
PMEGridSizeY     64
PMEGridSizeZ     64

```

```

# Constant Pressure Control (variable volume)
useGroupPressure      yes ;# needed for rigidBonds
useFlexibleCell       no
useConstantArea       no

langevinPiston        on
langevinPistonTarget  1.01325 ;# in bar -> 1 atm
langevinPistonPeriod  100
langevinPistonDecay    50
langevinPistonTemp     $temperature

# Output
outputName            $outputname
restartfreq           1000      ;# 1000steps = every 1ps
dcdfreq               125
xstFreq               1000
outputEnergies        500
outputPressure        500

#####
## EXTRA PARAMETERS                                     ##
#####

#####
## EXECUTION SCRIPT                                     ##
#####
minimize 7500
run 10200000

```

### A.3.2 Protein MD

```

#####
## JOB DESCRIPTION                                     ##
#####

# Minimization , Equilibration , and measuring pair interactions between

#####
## ADJUSTABLE PARAMETERS                               ##

```

```
#####
```

```
set simname          zinc_finger
```

```
amber                yes
```

```
parmfile             berg_dz.top
```

```
coordinates          berg_dz.pdb
```

```
bincoordinates       berg_dz.coor
```

```
binvelocities        berg_dz.vel
```

```
set temperature      298
```

```
set outputname       berg_dz
```

```
firsttimestep        0
```

```
#####
```

```
## SIMULATION PARAMETERS                                     ##
```

```
#####
```

```
# Force-Field Parameters
```

```
exclude              scaled1-4
```

```
1-4scaling           1.0
```

```
cutoff               12
```

```
switching            on
```

```
switchdist           10
```

```
pairlistdist         13.5
```

```
# Integrator Parameters
```

```
timestep              1.0  ;# 1fs/step
```

```
rigidBonds            all  ;# needed for 2fs steps
```

```
nonbondedFreq         1
```

```
fullElectFrequency    2
```

```
stepspercycle         10
```

```
# Constant Temperature Control
```

```
langevin              on    ;# do langevin dynamics
```

```
langevinDamping        5     ;# damping coefficient (gamma) of 5/ps
```

```
langevinTemp           $temperature
```

```
langevinHydrogen    off    ;# don't couple langevin bath to hydrogens
```

```
# Periodic Boundary Conditions
```

```
cellBasisVector1    47     0     0
```

```
cellBasisVector2     0    53     0
```

```
cellBasisVector3     0     0    47
```

```
cellOrigin           0     0     0
```

```
wrapAll              on
```

```
# PME (for full-system periodic electrostatics)
```

```
PME                  yes
```

```
PMEGridSizeX         64
```

```
PMEGridSizeY         64
```

```
PMEGridSizeZ         64
```

```
# Constant Pressure Control (variable volume)
```

```
useGroupPressure      yes ;# needed for rigidBonds
```

```
useFlexibleCell       no
```

```
useConstantArea       no
```

```
langevinPiston        on
```

```
langevinPistonTarget  1.01325 ;# in bar -> 1 atm
```

```
langevinPistonPeriod  200
```

```
langevinPistonDecay    100
```

```
langevinPistonTemp     $temperature
```

```
# Output
```

```
outputName            $outputname
```

```
restartfreq           500    ;# 500steps = every 1ps
```

```
dcdfreq               500
```

```
xstFreq               500
```

```
outputEnergies        10
```

```
outputPressure         10
```

```
#####
```

```
## EXTRA PARAMETERS ##
```

```
#####

#####
## EXECUTION SCRIPT ##
#####

minimize 10000
for { set TEMP 50 } { $TEMP < $temperature } { incr TEMP 50 } {
    reinitvels $TEMP
    langevinPistonTemp $TEMP
    langevinTemp $TEMP
    run 200
}
reinitvels $temperature
langevinPistonTemp $temperature
langevinTemp $temperature
run 5000000;
```

### A.3.3 Trajectory Analysis

```
#####
## JOB DESCRIPTION ##
#####

# Calculating Interaction Energies between zinc and water

#####
## ADJUSTABLE PARAMETERS ##
#####

set simname          MeOH_15

structure             $simname.psf
coordinates           $simname.pdb
extendedSystem        $simname.xsc

set temperature       298
set outputname        $simname.pair

firstTimestep         0
pairInteraction        on
```

```

pairInteractionGroup1 0
pairInteractionFile    $simname.meth.pdb
pairInteractionGroup2 1
pairInteractionCol      B
#####
## SIMULATION PARAMETERS                                     ##
#####

# Input
paraTypeCharmm          on
parameters               par.inp
temperature              $temperature

# Force-Field Parameters
exclude                  scaled1-4
1-4scaling               1.0
cutoff                   12
switching                on
switchdist               10
pairlistdist             13.5
COMmotion                 yes

# Periodic Boundary Conditions
cellBasisVector1        36    0    0
cellBasisVector2         0   36    0
cellBasisVector3         0    0   36
cellOrigin               0    0    0

wrapAll                  on

# PME (for full-system periodic electrostatics)
PME                      yes
PMEGridSizeX             64
PMEGridSizeY             64
PMEGridSizeZ             64

# Output
outputName               $outputname
#####

```

```

## EXTRA PARAMETERS                                     ##
#####

#####

## EXECUTION SCRIPT                                     ##
#####

set ts 0
coorfile open dcd $simname.dcd
while { ![coorfile read] } {
    firstTimestep $ts
    run 0
    incr ts 1
}
coorfile close

```

## A.4 NWCHEM Input files

### A.4.1 Preparation

```

#Creates files for optimization of the berg zinc fingerG

start berg
prepare
system berg
source berg_orig.pdb
new_top new_rst
center
orient
solvate 5.0
modify atom 202:ZN quantum
modify atom 45:_CB quantum
modify atom 45:3HB quantum
modify atom 45:2HB quantum
modify atom 45:_SG quantum
modify atom 50:_CB quantum
modify atom 50:3HB quantum
modify atom 50:2HB quantum
modify atom 50:_SG quantum
modify atom 63:_NE2 quantum

```

```

modify atom 63:_CG quantum
modify atom 63:_ND1 quantum
modify atom 63:_CE1 quantum
modify atom 63:_CD2 quantum
modify atom 63:_HD2 quantum
modify atom 63:_HE1 quantum
modify atom 63:_HD1 quantum
modify atom 67:_NE2 quantum
modify atom 67:_CG quantum
modify atom 67:_ND1 quantum
modify atom 67:_CE1 quantum
modify atom 67:_CD2 quantum
modify atom 67:_HD2 quantum
modify atom 67:_HE1 quantum
modify atom 67:_HD1 quantum
update lists
ignore
write berg.rst
write berg.pdb
end

```

```
task prepare
```

## A.4.2 Optimization

```

memory total 8192 mb
scratch_dir scratch
start berg

```

```

# LANL2DZ ECP EMSL Basis Set Exchange Library 2/8/12 1:45 PM
# Elements References
# -----
# H - Ne: T. H. Dunning Jr. and P. J. Hay, in Methods of Electronic Structure
# Theory, Vol. 2, H. F. Schaefer III, ed., PLENUM PRESS (1977)
# Na - Hg: P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 270 (1985).
# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 284 (1985).
# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 299 (1985).
#

BASIS "ao basis" PRINT
#BASIS SET: (4s) -> [2s]
H S

```



	19.2384000	0.0328280
	2.8987000	0.2312040
	0.6535000	0.8172260
H	S	
	0.1776000	1.0000000
#BASIS SET: (10s,5p) -> [3s,2p]		
C	S	
	4233.0000000	0.0012200
	634.9000000	0.0093420
	146.1000000	0.0454520
	42.5000000	0.1546570
	14.1900000	0.3588660
	5.1480000	0.4386320
	1.9670000	0.1459180
C	S	
	5.1480000	-0.1683670
	0.4962000	1.0600910
C	S	
	0.1533000	1.0000000
C	P	
	18.1600000	0.0185390
	3.9860000	0.1154360
	1.1430000	0.3861880
	0.3594000	0.6401140
C	P	
	0.1146000	1.0000000
#BASIS SET: (10s,5p) -> [3s,2p]		
N	S	
	5909.0000000	0.0011900
	887.5000000	0.0090990
	204.7000000	0.0441450
	59.8400000	0.1504640
	20.0000000	0.3567410
	7.1930000	0.4465330
	2.6860000	0.1456030
N	S	
	7.1930000	-0.1604050
	0.7000000	1.0582150
N	S	
	0.2133000	1.0000000
N	P	

	26.7900000	0.0182540
	5.9560000	0.1164610
	1.7070000	0.3901780
	0.5314000	0.6371020
N	P	
	0.1654000	1.0000000
#BASIS SET: (3s,3p) -> [2s,2p]		
S	S	
	1.8500000	-0.5324335
	0.4035000	1.2763801
S	S	
	0.1438000	1.0000000
S	P	
	4.9450000	-0.0608116
	0.4870000	1.0132686
S	P	
	0.1379000	1.0000000
#BASIS SET: (3s,2p,5d) -> [2s,2p,2d]		
Zn	S	
	0.7997000	-0.6486112
	0.1752000	1.3138291
Zn	S	
	0.0556000	1.0000000
Zn	P	
	0.1202000	1.0000000
Zn	P	
	0.0351000	1.0000000
Zn	D	
	68.8500000	0.0258532
	18.3200000	0.1651195
	5.9220000	0.4468212
	1.9270000	0.5831080
Zn	D	
	0.5528000	1.0000000

END

# Elements

References

# \_\_\_\_\_

\_\_\_\_\_

# Na - Hg: P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 270 (1985).

# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 284 (1985).

# P. J. Hay and W. R. Wadt, J. Chem. Phys. 82, 299 (1985).

#

ECP		
S nelec 10		
S ul		
1	532.6685222	-10.0000000
2	108.1342248	-85.3593846
2	24.5697664	-30.4513290
2	7.3702438	-10.3745886
2	2.3712569	-0.9899295
S S		
0	106.3176781	3.0000000
1	100.8245833	10.6284036
2	53.5858472	223.6360469
2	15.3706332	93.6460845
2	3.1778402	28.7609065
S P		
0	101.9709185	5.0000000
1	93.2808973	6.0969842
2	65.1431772	285.4425500
2	24.6347440	147.1448413
2	7.8120535	53.6569778
2	2.3112730	8.9249559
Zn nelec 18		
Zn ul		
1	386.7379660	-18.0000000
2	72.8587359	-124.3527403
2	15.9066170	-30.6601822
2	4.3502340	-10.6358989
2	1.2842199	-0.7683623
Zn S		
0	19.0867858	3.0000000
1	5.0231080	22.5234225
2	1.2701744	48.4465942
2	1.0671287	-44.5560119
2	0.9264190	12.9983958
Zn P		
0	43.4927750	5.0000000
1	20.8692669	20.7435589
2	21.7118378	90.3027158
2	6.3616915	74.6610316

```

2      1.2291195      9.8894424
Zn D
2      13.5851800     -4.8490359
2      9.8373050      3.6913379
2      0.8373113     -0.5037319
END

dft
      xc b3lyp
end

md
      system berg
      noshake
end

qmmm
      bqzone 9
      region qm      mm      solvent
      maxiter 500      10000      50000
      ncycles 10
      density static
      xyz berg.optim
end

task qmmm dft optimize

```

## B Calculation Scripts

### B.1 Radial Distribution Function

VMD code:

```

mol new PPP
mol addfile DDD type dcd first FFF waitfor all
set ion [atomselect top "resname ZN2"]
$ion num
set meth_o [atomselect top "name O and pbwithin 15 of resname ZN2"]
$meth_o num
set meth_c [atomselect top "name C and pbwithin 15 of resname ZN2"]
$meth_c num

```

```

set wat_o [atomselect top "name OH2 and pbwithin 15 of resname ZN2"]
$wat_o num
set frames [molinfo 0 get numframes]
set frames [expr "$frames - 1"]
puts $frames
set res_o [measure gofr $ion $meth_o delta 0.1 rmax 10 first 0 last $frames usepb true selupdate t
set res_c [measure gofr $ion $meth_c delta 0.1 rmax 10 first 0 last $frames usepb true selupdate t
set wat_o [measure gofr $ion $wat_o delta 0.1 rmax 10 first 0 last $frames usepb true selupdate tr
set out [open "OOO" w]
puts $out $res_o
puts $out $res_c
puts $out $wat_o
close $out

```

## MATLAB Code

```

%Reads a gofr file generated from VMD and
%plots the radial distribution function
function plot_gofr(filename)
A=importdata(sprintf('%s.gofr.fmt',filename), '_');
plot(A(1,:), A(4,:), '-k', A(5,:), A(8,:), '-b', A(9,:), A(12,:), '-.g', 'LineWidth',5)
lh=legend('Zn-MeO', 'Zn-MeC', 'Zn-H2O')
set(lh, 'FontSize',30);
xlabel('r_(Angstroms)', 'FontSize',30)
ylabel('g(r)', 'FontSize',30);
axis([0 6 0 3]);
set(gca, 'FontSize',30);
print(sprintf('thesis_plots/%s_gofr.png', filename), '-dpng', '-r300');
end

```

## B.2 Occupancy Probability

```

mol new PPP
mol addfile DDD type dcd first BBB waitfor all
set wat_o [atomselect top "name OH2 and (pbwithin OOO of resname ZN2) and (not pbwithin III of resname ZN2)"]
set meth_o [atomselect top "name O and (pbwithin OOO of resname ZN2) and (not pbwithin III of resname ZN2)"]
$meth_o num
set meth_c [atomselect top "name C and (pbwithin OOO of resname ZN2) and (not pbwithin III of resname ZN2)"]
$meth_c num
for {set counter 0} {$counter < 30} {incr counter} {
    lappend wat_o_ctr 0
}

```

```

        lappend meth_o_ctr 0
        lappend meth_c_ctr 0
        lappend num $counter
    }
    set frames [molinfo 0 get numframes]
    for {set counter 0} {$counter < $frames } {incr counter} {
        $wat_o frame $counter
        $meth_o frame $counter
        $meth_c frame $counter
        $wat_o update
        $meth_o update
        $meth_c update
        set wat_o_ind [$wat_o num]
        if {$wat_o_ind >= [llength $wat_o_ctr]} {set $wat_o_ind [expr [llength $wat_o_ctr] - 1]}
        set meth_o_ind [$meth_o num]
        if {$meth_o_ind >= [llength $meth_o_ctr]} {set $meth_o_ind [expr [llength $meth_o_ctr] - 1]}
        set meth_c_ind [$meth_c num]
        if {$meth_c_ind >= [llength $meth_c_ctr]} {set $meth_c_ind [expr [llength $meth_c_ctr] - 1]}

        set wat_o_ctr [lreplace $wat_o_ctr $wat_o_ind $wat_o_ind [expr [lindex $wat_o_ctr $wat_o_ind] - 1]]
        set meth_o_ctr [lreplace $meth_o_ctr $meth_o_ind $meth_o_ind [expr [lindex $meth_o_ctr $meth_o_ind] - 1]]
        set meth_c_ctr [lreplace $meth_c_ctr [$meth_c num] [$meth_c num] [expr [lindex $meth_c_ctr $meth_c_ind] - 1]]
    }
    set out [open 'WWW' w]
    puts $out $num
    puts $out $wat_o_ctr
    puts $out $meth_o_ctr
    puts $out $meth_c_ctr
    close $out

```

### B.3 MD Free energy

After using the pair interaction energy script (Appendix A.3.3), the nrg file is further processed

```

#!/usr/bin/perl -w
my($input, $title, $output)=@ARGV;
print "
A=importdata(' $input ');
allnrg=A(50:17500,:); \%interaction energy

```

```

intnrg=allnrg (:,6);
elec=allnrg (:,3);
vdw=allnrg (:,4);
mean(intnrg)
std(intnrg)
beta=1/0.593; \%in kcal/mol
G=mean(intnrg)+var(intnrg)/2*beta;
B=exp(intnrg * beta);
C=sum(B) ./ length(B); \%This is the sum over the probabilities
D=log(C) / beta \%solving e^(b*mu) for mu
[E,F]=hist(intnrg, 150);
E=E/sum(E);
[thefit,thegof]=fit(F', E', 'gauss1')
semilogy(F,E,'ob')
hold on
semilogy(F, feval(thefit, F'));
xlabel('Pair interaction energy (kcal/mol)')
ylabel('Probability')
\%title(sprintf('Zn^{2+}/non-first-shell interaction energies, $title. \mu^{ex}_{calc}=%6.4f kcal/mol')
axis([min(F)-10, max(F)+10, min(E),max(E)]);
print('-djpeg', '$output.hist.jpg');
disp('\n')
disp(sprintf('Approx: %6.4f-Gaussian: %6.4f-%6.4f-%6.4f-%6.4f-%6.4f',D,G,mean(elec), var(elec), mean(elec)))

```

## C Results

### C.1 Radial distribution functions

### C.2 MD Interaction Energy Histograms

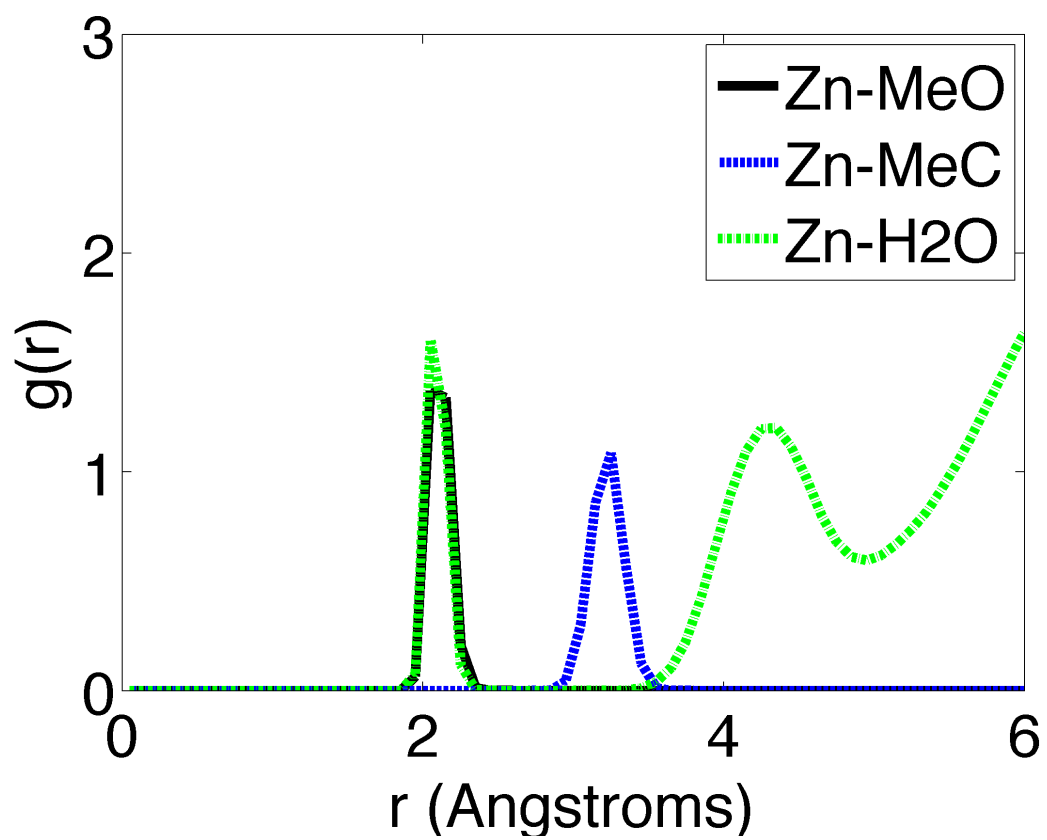


Figure 11:  $Zn^{2+} [H_2O]_3 [MeOH]_3$  in water



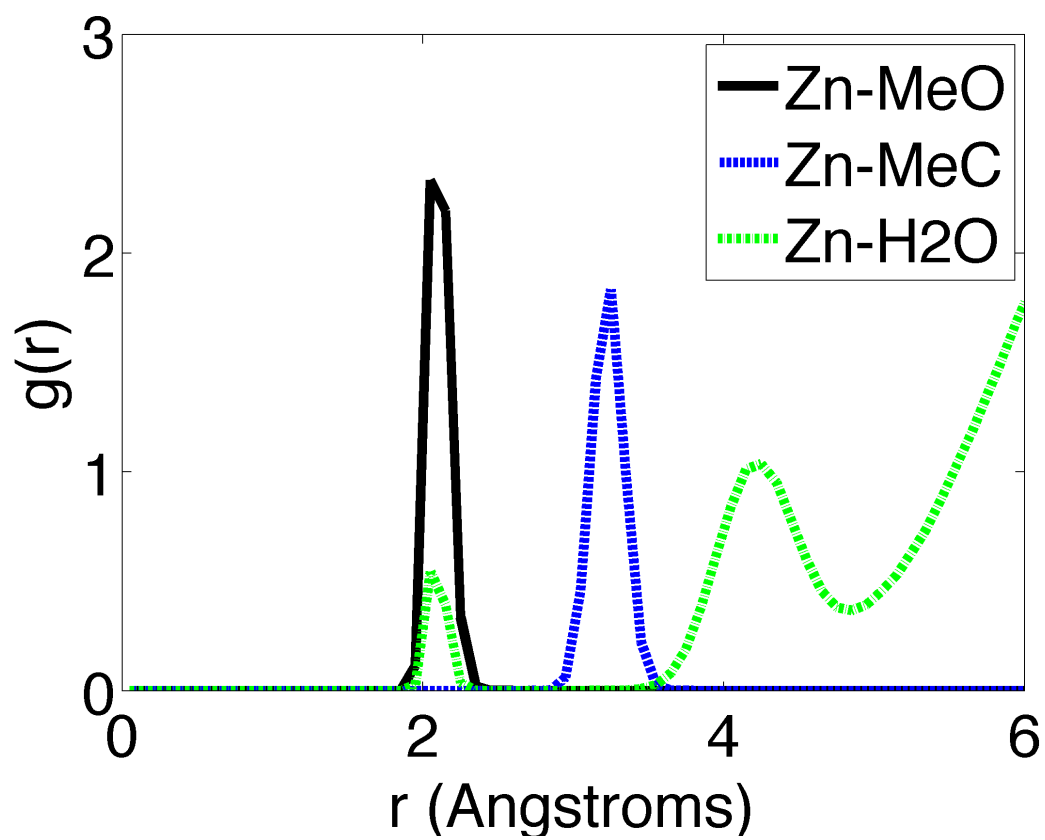


Figure 12:  $Zn^{2+} [H_2O]_1 [MeOH]_5$  in water

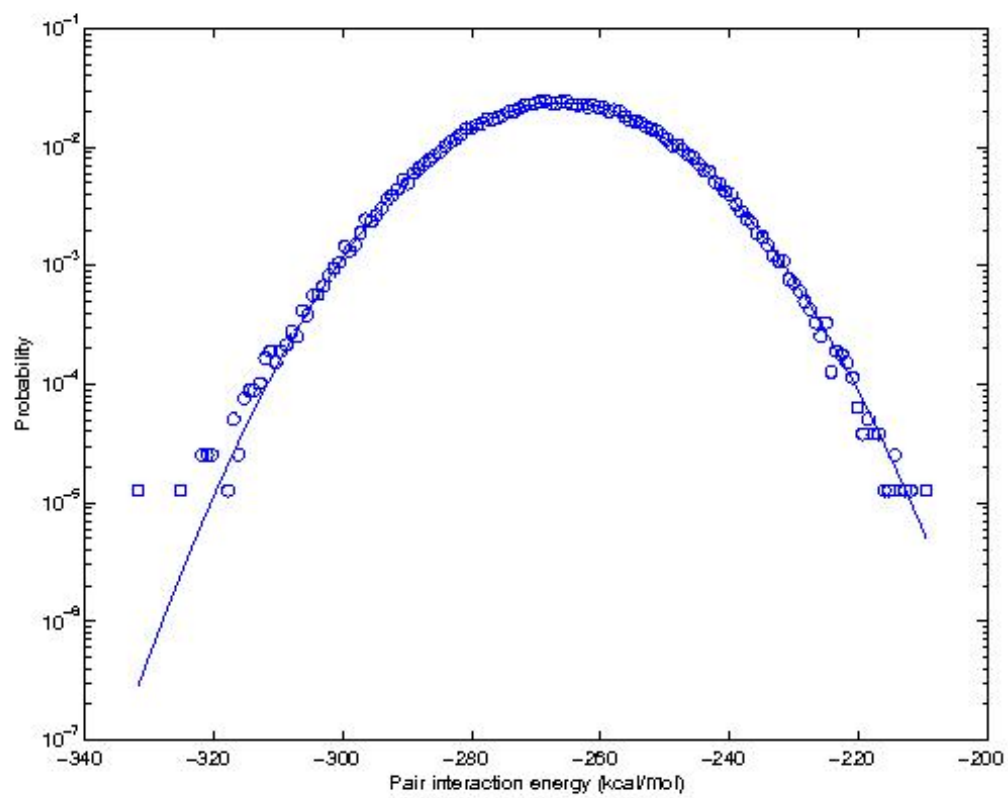


Figure 13:  $Zn^{2+} [H_2O]_4 [MeOH]_2$  in water

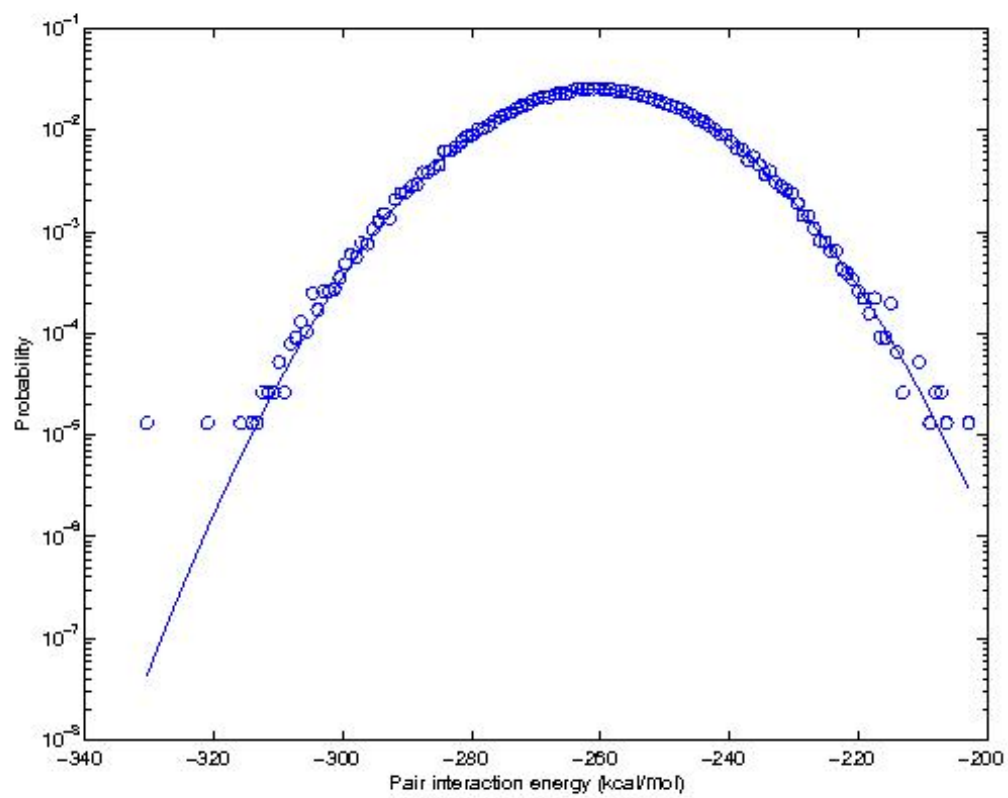


Figure 14:  $Zn^{2+} [H_2O]_3 [MeOH]_3$  in water

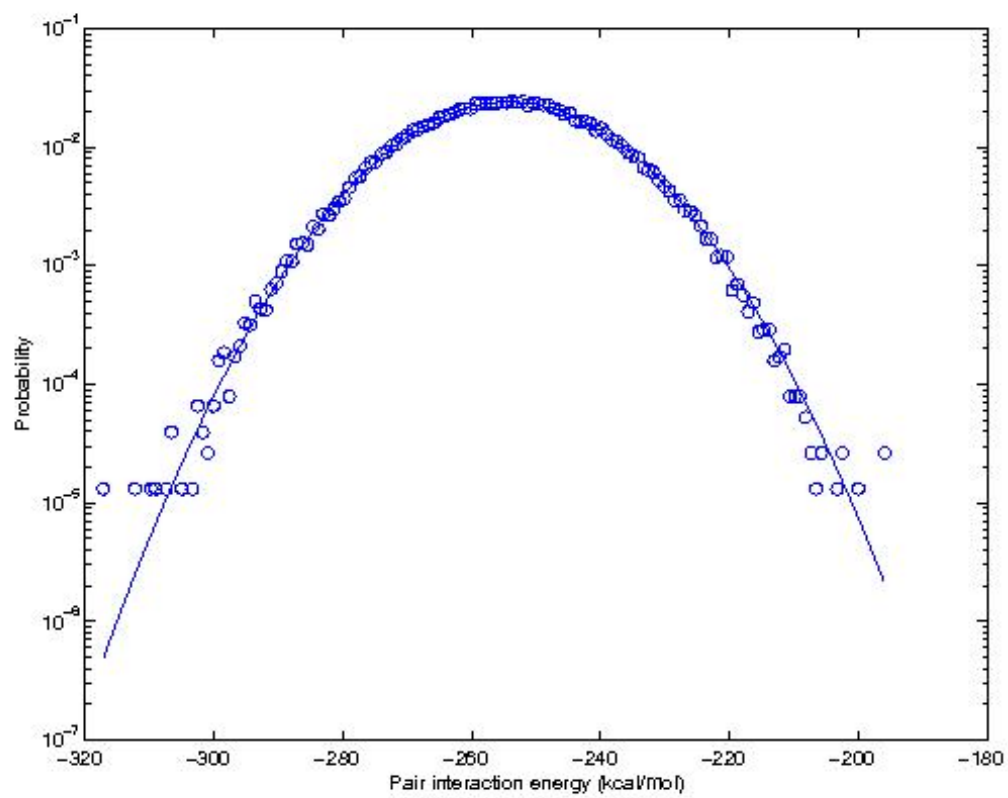


Figure 15:  $Zn^{2+} [H_2O]_2 [MeOH]_4$  in water

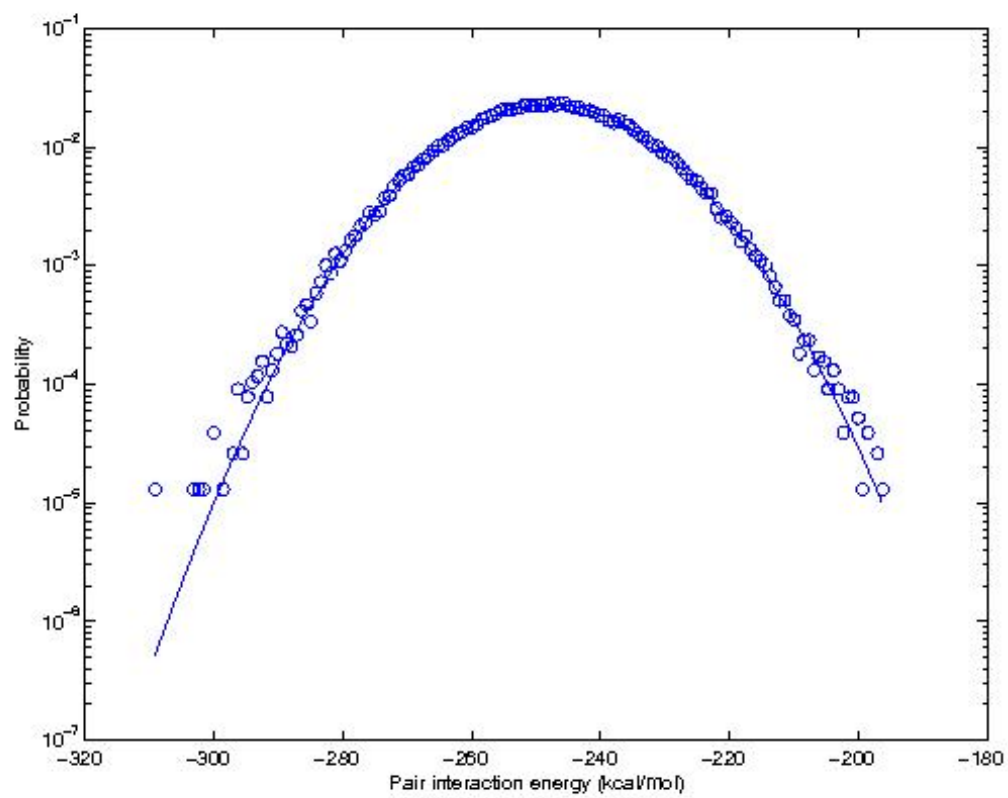


Figure 16:  $Zn^{2+} [H_2O]_1 [MeOH]_5$  in water

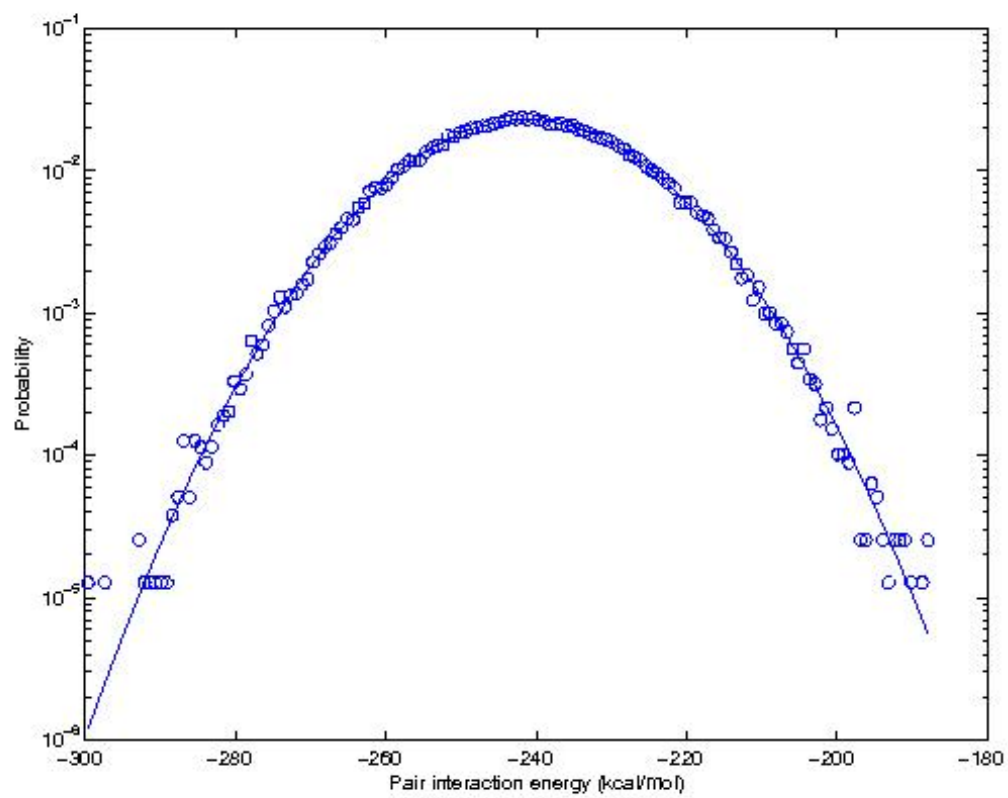


Figure 17:  $Zn^{2+} [H_2O]_0 [MeOH]_6$  in water

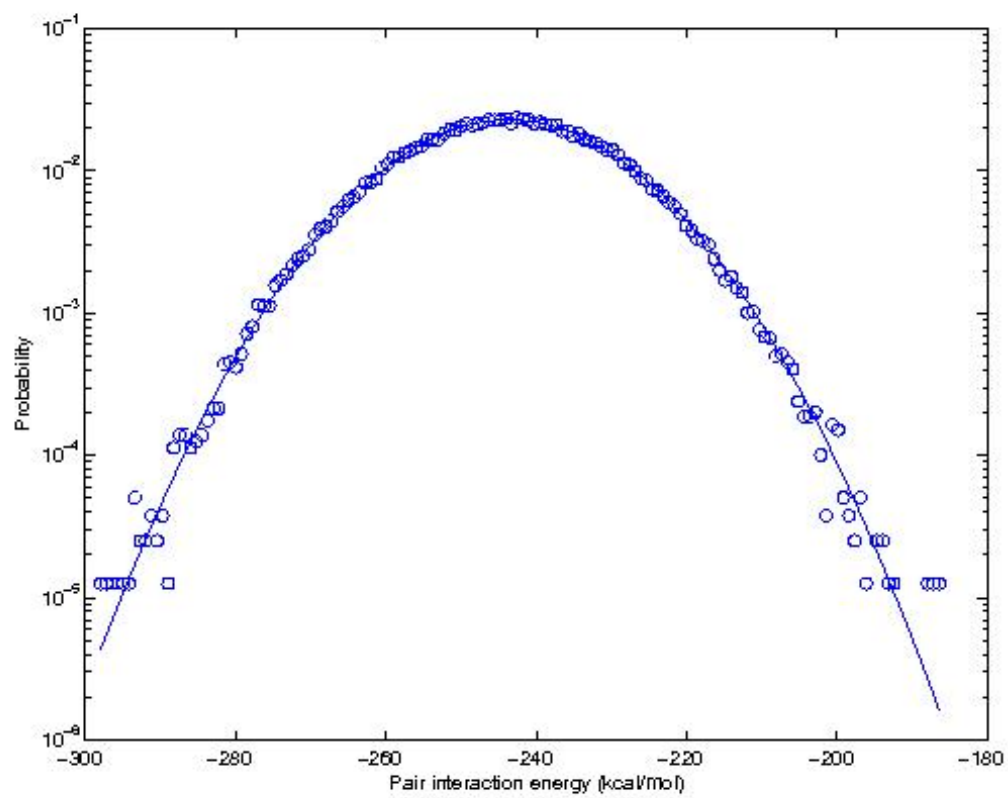


Figure 18:  $Zn^{2+} [H_2O]_0 [MeOH]_6$  in 5% MeOH and water

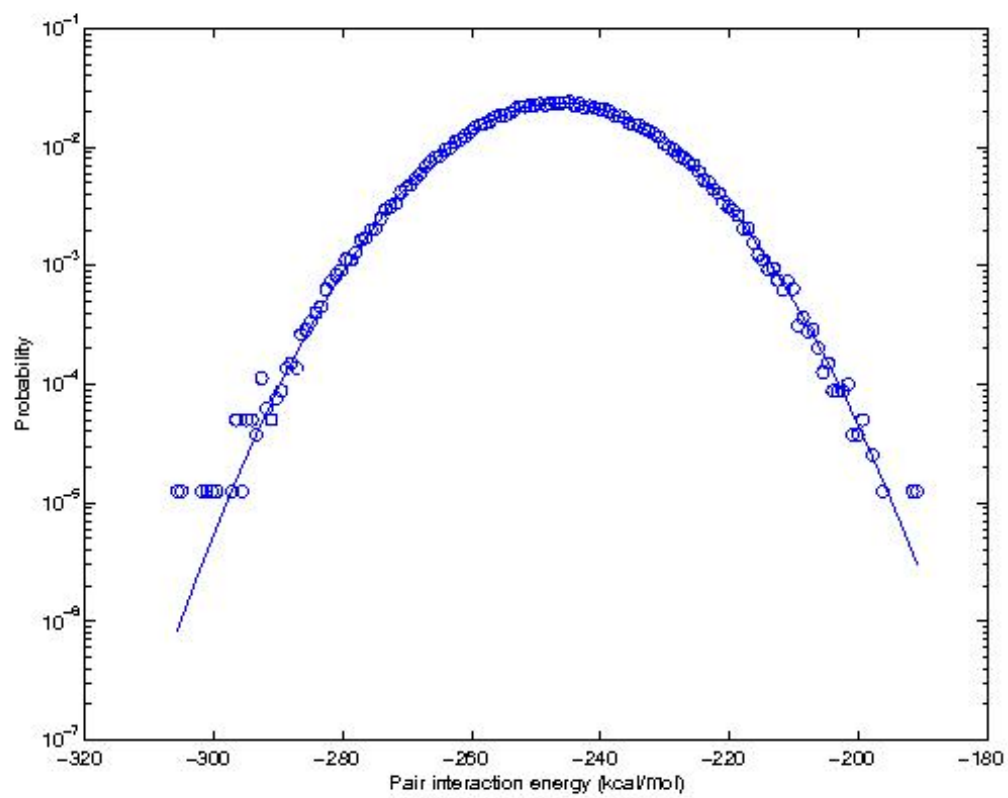


Figure 19:  $Zn^{2+} [H_2O]_0 [MeOH]_6$  in 10% MeOH and water



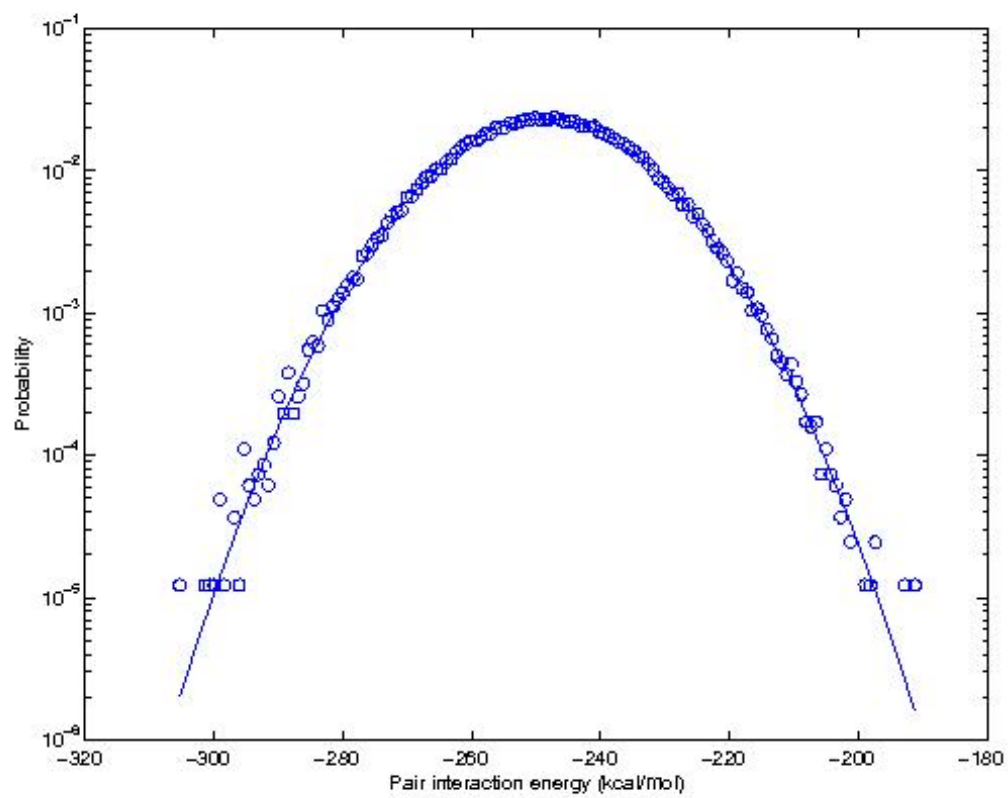


Figure 20:  $Zn^{2+} [H_2O]_0 [MeOH]_6$  in 15% MeOH and water